



St Mary's Church of England Primary School



Mathematics Curriculum Progression Document

*"Through the loving example of Jesus Christ we strive to provide opportunities for all members of our **diverse** school community to **flourish** within a **caring, aspirational, spiritual** and **inclusive** environment. We aim to create **successful** learners, **confident** individuals and **responsible citizens** ready to take the next steps in life"*

Peace



Friendship



Respect



Trust



Perseverance



Maths Curriculum Intent, Implementation and Impact

Intent

Mathematics is an important creative discipline that helps us to understand and act as **responsible citizens** to change the world; we want our children to know the purpose behind their learning and apply their **aspirational** knowledge to life. We want all pupils at **St Mary's Primary School** to experience the beauty, power and enjoyment of mathematics and develop a sense of curiosity about the subject with a clear and **confident** understanding.

At **St Mary's Primary School**, we value a **diverse** and **inclusive** maths curriculum that is creative and engaging; this curriculum is accessible to all children, enabling them to **flourish**. We believe all children can achieve in mathematics; we foster positive 'can do'/**caring** attitudes, and teach for secure and **deep understanding** of numerical concepts through manageable steps. We use mistakes and misconceptions as an essential and **intellectual** part of learning and provide challenge through rich and sophisticated questioning. Our children need to develop the necessary skills to make them "deep thinkers" acquiring maths skills that can be recalled quickly and transferred and applied in different contexts. They need to be able to make purposeful connections across the areas of maths and use their knowledge in other subjects.

At St Mary's, we use and follow the *White Rose Primary Scheme of Learning* to secure and deepen their understanding, with a range of manipulatives to enhance the teaching and learning. They will spend time becoming true masters of content, applying and being creative with new knowledge in multiple ways. In EYFS we use the NCETM 'Mastering Number' programme to teach Mathematics. In Year 1 and 2 the 'Mastering Number' programme is used in addition to the White Rose Primary Scheme of learning.

We aim for all pupils to:

- ✓ become fluent in the fundamentals of mathematics so that they develop conceptual understanding and the ability to recall and apply knowledge rapidly and accurately.
- ✓ be able to solve problems by applying their mathematics to a variety of problems with increasing sophistication, including in unfamiliar contexts and to model real-life scenarios.
- ✓ reason mathematically by following a line of enquiry and develop and present a justification, argument or proof using mathematical language or representations.
- ✓ have an appreciation of number and number operations, which enables mental calculations and written procedures to be performed efficiently, fluently and accurately to be successful in mathematics.

Implementation

At St Mary's, we strive to provide a wide variety of teaching approaches, through the White Rose Curriculum, to ensure children make good progress. Maths lessons will follow a clear and consistent teaching sequence, allowing children to develop into confident and successful Mathematicians.

- Scheme of work: We use the White Rose Primary Scheme of Learning and the 'Mastering Number' programme as a solid foundation of our teaching and learning, which is in line with the National Curriculum.
- Provision in EYFS: Children are given a secure grounding in the phases of learning, ensuring they have a good foundation on which to build through the specific areas, including the key principles outlined in the scheme. Areas of provision are enhanced to ensure vocabulary understanding and extension, and develop key mathematical concepts and special thinking.
- Fluency is developed through repeating, reinforcing and revising key skills; daily arithmetic takes place in all classes. Children are given time to practice and perfect their calculation strategies including giving pupils the opportunity to make appropriate decisions when estimating, calculating and evaluating the effectiveness of their chosen methods.
- Staff subject knowledge allows the intentions of our mathematics curriculum to be delivered successfully. We continually strive to build upon the understanding of the expectations of the curriculum that our staff have, through quality CPD which is provided through the subject leader and external courses. All staff are encouraged to raise questions, seek support and request further training if needed in order to ensure everyone is confident in what they teach. Good practice is always shared between staff and all CPD is used to inform teaching and learning across school.
- Maths Display: Each class has a display/'Working Wall' which includes key knowledge/vocabulary and examples linked to the area of maths.
- Correct mathematical vocabulary is used by all teachers and this is discussed with, and explained, to children who are then encouraged to use it independently when talking about maths. Vocabulary is displayed clearly on working walls and is referred to in every lesson. Stem sentences are provided to guide and support the children with explanations.
- Assessment: Class teachers assess children's understanding in maths using the 21 Steps Assessment programme of study document, 21 Steps provides a systematic approach to assessing and informing pupils' mathematical learning over time: starting with the EYFS Early Learning Goals and the National Curriculum for each year group from YR to Y6 which has been broken down into progressive steps.

- Feedback is given in a variety of ways to ensure pupils are well informed and making visible progress. Green highlighter portrays correct understanding and pink (think pink) highlights areas for development. Discussion is essential to learning and children are encouraged to discuss their thoughts, ideas and methods with a partner, group or the teacher. Children work both collaboratively and independently when solving problems which require them to persevere and develop resilience
- Timetabled interventions for maths are in place for children with SEND in all classes; all other children receive regular group support as part of their maths lessons with further support for individuals or small groups where a need is identified.
- Resources and equipment are audited so that children have materials of high quality and accuracy to support their learning. Our resources allow us to better use models and images to support learning in each area.

Impact

- All children will achieve age related expectations in Maths, with exception of some linked personalised plans.
- Children know that maths is a vital life skill that they will rely on in many areas of their daily life.
- Children have an opportunity to strengthen and deepen their mathematical understanding and abilities.
- Children will have opportunities to practice, question, apply and reflect on what they have learnt.
- Children will have opportunities to explore, working practically and collaboratively to deepen their understanding.
- Children will be able to confidently explain their mathematical learning journey.

Subject Leader – Mrs Emma Fagg

Mastering Number Weekly Overview

Reception

Week	Strand	Content
1	Subitising	Perceptual subitising to 3
2	Counting	Counting sequence; 1:1 correspondence, cardinality
3	Composition	Composition of 3 and 4; all numbers can be made of ones
4	Subitising	Subitising to 4; perceptual and conceptual; making 4
5	Comparison	Focus on language and thinking about attributes
6	Cardinality and counting	Focus on counting to 5 and the key representation of '5 fingers on one hand', and the die-five pattern
7	Comparison	Comparison by matching, including when groups are equal
8	Composition	Focus on the concept of a 'whole'
9	Composition	Focus on the composition of 5
10	Cardinality and counting	Counting beyond 5
11	Subitising	Connect subitised quantities to numerals
12	Ordinality	Order numbers to 5 Focus on each number being 1 more than the previous number
13	Composition	Focus on the composition of 5 and identify missing parts
14	Composition	Introduce the '5 and a bit' structure using fingers and die frames as key representations
15	Comparison	Focus on equal and unequal groups
16	Counting	Connect the counting sequence to ordinality. Connect ordinality and cardinality through the use of the 'staircase' pattern and explore '1 more' and '1 less'
17	Comparison	Comparison using knowledge of ordinality rather than comparison by matching of quantities Focus on noticing whether a change creates a number which is more or less than another
18	Composition	Composition of 7 as 2 groups, with a focus on '5 and a bit'
19	Subitising	Practise subitising within 6 Explore doubles
20	Composition	Sort odd and even numbers by looking at their tops; odd blocks and flat tops

21	Counting, cardinality and ordinality	Count larger amounts and focus on strategies for counting
22	Subitising	Focus on structured arrangements including the 10-frame
23	Composition	Focus on representations of numbers using fingers and 10-frames
24	Composition	Focus on doubles using different representations
25	Comparison	Focus on ordinality: comparing numbers
26	Subitising and the rekenrek	'Seeing' small quantities and numbers within larger quantities Introduction to the rekenrek Link familiar representations such as numbers of fingers to representations on the rekenrek
27	Counting	Strategies for counting Recognise the pattern of the counting system when beginning to count beyond 20
28	Comparison	Compare groups of objects that are of different sizes/colours/attributes Develop a sense of magnitude e.g., knowing that 8 is a lot more than 2, but that 4 is only a little bit more than 2
29	Pattern in number	Investigate 'parts' and 'wholes' Explore the composition of numbers to 10 Investigate equivalence, doubles and making odd and even numbers
30	Deep understanding of numbers to 10	Continue to practically explore the composition of numbers to 10 Investigate 5 as a key 'anchor' in the number system Begin to generalise about 1 more/1 less within 10
31	Recall of number facts	Recall the 'numbers within' 3, 4, 5 and 10 Recall double facts, up to '5 and 5 make 10' Recall missing parts within 5

Place value: Count

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
- count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number - Count numbers to 100 in numerals; count in multiples of twos, fives and tens	count in steps of 2, 3, and 5 from 0, and in tens from any number, forward and backward	count from 0 in multiples of 4, 8, 50 and 100; find 10 or 100 more or less than a given number	- count in multiples of 6, 7, 9, 25 and 1000 - count backwards through zero to include negative numbers	- count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000 - count forwards and backwards with positive and negative whole numbers, including through zero	
Autumn 1 Spring 1 Spring 3 Summer 4	Autumn 1	Autumn 1 Autumn 3	Autumn 1 Autumn 4	Autumn 1 Summer 4	

Place value: Represent

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
- identify and represent numbers using objects and pictorial representations - read and write numbers to 100 in numerals - read and write numbers from 1 to 20 in numerals and words	- read and write numbers to at least 100 in numerals and in words - identify, represent and estimate numbers using different representations, including the number line	- identify, represent and estimate numbers using different representations - read and write numbers up to 1000 in numerals and in words	- identify, represent and estimate numbers using different representations - read Roman numerals to 100 (I to C) and know that over time, the numeral system changed to include the concept of zero and place value	- read, write, (order and compare) numbers to at least 1 000 000 and determine the value of each digit - read Roman numerals to 1000 (M) and recognise years written in Roman numerals	read, write, (order and compare) numbers up to 10 000 000 and determine the value of each digit
Autumn 1 Spring 1 Spring 3 Summer 4	Autumn 1	Autumn 1	Autumn 1	Autumn 1	Autumn 1

Place value: Use and compare

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
given a number, identify one more and one less	- recognise the place value of each digit in a two-digit number (tens, ones) - compare and order numbers from 0 up to 100; use $<$, $>$ and $=$ signs	- recognise the place value of each digit in a three-digit number (hundreds, tens, ones) - compare and order numbers up to 1000	- find 1000 more or less than a given number - recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones) - order and compare numbers beyond 1000	(read, write) order and compare numbers to at least 1 000 000 and determine the value of each digit	(read, write), order and compare numbers up to 10 000 000 and determine the value of each digit
Autumn 1 Spring 1 Spring 3 Summer 4	Autumn 1	Autumn 1	Autumn 1	Autumn 1	Autumn 1

Place value: Problems/Rounding

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
	use place value and number facts to solve problems	solve number problems and practical problems involving these ideas	- round any number to the nearest 10, 100 or 1000 - solve number and practical problems that involve all of the above and with increasingly large positive numbers	- interpret negative numbers in context - round any number up to 1 000 000 to the nearest 10, 100, 1000, 10 000 and 100 000 - solve number problems and practical problems that involve all of the above	- round any whole number to a required degree of accuracy - use negative numbers in context, and calculate intervals across zero - solve number and practical problems that involve all of the above
	Autumn 1	Autumn 1	Autumn 1	Autumn 1	Autumn 1

Addition & subtraction: Calculations

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
add and subtract one-digit and two-digit numbers to 20, including zero	- add and subtract numbers using concrete objects, pictorial representations, and mentally, including: - a two-digit number and ones - a two-digit number and tens - two two-digit numbers - adding three one-digit numbers	- add and subtract numbers mentally, including: - a three-digit number and ones - a three-digit number and tens - a three-digit number and hundreds - add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction	add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate	- add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction) - add and subtract numbers mentally with increasingly large numbers	- perform mental calculations, including with mixed operations and large numbers - use their knowledge of the order of operations to carry out calculations involving the four operations
Autumn 2 Spring 2	Autumn 2	Autumn 2	Autumn 2	Autumn 2	Autumn 2

Addition & subtraction: Problems

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
• solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as $7 = \square - 9$	• solve problems with addition and subtraction: ➤ using concrete objects and pictorial representations, including those involving numbers, quantities and measures ➤ applying their increasing knowledge of mental and written methods	• solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction	• solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why	• solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why • solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign	• solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why
Autumn 2 Spring 2	Autumn 2	Autumn 2	Autumn 2	Autumn 2	Autumn 2

Multiplication & division: Recall/Use

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
	- recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers - show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot	recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables	- recall multiplication and division facts for multiplication tables up to 12×12 - use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1; dividing by 1; multiplying together three numbers - recognise and use factor pairs and commutativity in mental calculations	- identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers - know and use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers - establish whether a number up to 100 is prime and recall prime numbers up to 19 - recognise and use square numbers and cube numbers, and the notation for squared (2) and cubed (3)	- identify common factors, common multiples and prime numbers - use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy
	Spring 2	Autumn 3 Spring 1	Autumn 4 Spring 1	Autumn 3	Autumn 2

Multiplication & division: Calculations

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
	calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication ($\times$), division ($\div$) and equals (=) signs	write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods	multiply two-digit and three-digit numbers by a one-digit number using formal written layout	- multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers - multiply and divide numbers mentally drawing upon known facts - divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context - multiply and divide whole numbers and those involving decimals by 10, 100 and 1000	- multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication - divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context - divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context - perform mental calculations, including with mixed operations and large numbers
	Spring 2	Autumn 3 Spring 1	Spring 1	Autumn 3 Spring 1	Autumn 2

Multiplication & division: Problems

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher	solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts	solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects	solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects	- solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes - solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates	solve problems involving addition, subtraction, multiplication and division
Summer 1	Spring 2	Spring 1	Spring 1	Autumn 3 Spring 1	Autumn 2

Multiplication & division: Combined

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
				solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign	use their knowledge of the order of operations to carry out calculations involving the four operations
				Spring 1	Autumn 2

Fractions: Recognise and write

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
- recognise, find and name a half as one of two equal parts of an object, shape or quantity - recognise, find and name a quarter as one of four equal parts of an object, shape or quantity	recognise, find, name and write fractions $\frac{1}{3}$, $\frac{1}{4}$, $\frac{2}{4}$ and $\frac{3}{4}$ of a length, shape, set of objects or quantity	- count up and down in tenths; recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10 - recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators - recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators	count up and down in hundredths; recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten.	- identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths - recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1 as a mixed number [for example, $\frac{2}{5} + \frac{4}{5} = \frac{6}{5} = 1\frac{1}{5}$]	
Summer 2	Summer 1	Spring 3	Spring 4 Summer 1	Autumn 4	

Fractions: Compare

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
	Recognise the equivalence of $\frac{2}{4}$ and $\frac{1}{2}$	- recognise and show, using diagrams, equivalent fractions with small denominators - compare and order unit fractions, and fractions with the same denominators	recognise and show, using diagrams, families of common equivalent fractions	compare and order fractions whose denominators are all multiples of the same number	- use common factors to simplify fractions; use common multiples to express fractions in the same denomination - compare and order fractions, including fractions > 1
	Summer 1	Spring 3	Spring 3	Autumn 4	Autumn 3

Fractions: Calculations

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
	write simple fractions for example, $\frac{1}{2}$ of 6 = 3	add and subtract fractions with the same denominator within one whole [for example, $\frac{5}{7} + \frac{1}{7} = \frac{6}{7}$]	add and subtract fractions with the same denominator	- add and subtract fractions with the same denominator and denominators that are multiples of the same number - multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams	- add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions - multiply simple pairs of proper fractions, writing the answer in its simplest form [for example, $\frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$] - divide proper fractions by whole numbers [for example $\frac{1}{3} \div 2 = \frac{1}{6}$]
	Summer 1	Summer 1	Spring 3	Autumn 4 Spring 2	Autumn 3 Autumn 4

Fractions: Solve problems

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
		solve problems that involve all of the above	solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number		
		Spring 3 Summer 1	Spring 3		

Decimals: Recognise, write, compare

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
			- recognise and write decimal equivalents of any number of tenths or hundredths - recognise and write decimal equivalents to $\frac{1}{4}, \frac{1}{2}, \frac{3}{4}$ - round decimals with one decimal place to the nearest whole number - compare numbers with the same number of decimal places up to two decimal places	- read and write decimal numbers as fractions [for example, $0.71 = \frac{71}{100}$] - recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents - round decimals with two decimal places to the nearest whole number and to one decimal place - read, write, order and compare numbers with up to three decimal places	identify the value of each digit in numbers given to three decimal places
			Spring 4 Summer 1	Spring 3 Summer 3	Spring 3

Fractions, decimals and percentages

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
			solve simple measure and money problems involving fractions and decimals to two decimal places	- recognise the per cent symbol (%) and understand that per cent relates to 'number of parts per hundred', and write percentages as a fraction with denominator 100, and as a decimal - solve problems which require knowing percentage and decimal equivalents of $\frac{1}{2}, \frac{1}{4}, \frac{1}{5}, \frac{2}{5}, \frac{4}{5}$ and those fractions with a denominator of a multiple of 10 or 25	- associate a fraction with division and calculate decimal fraction equivalents [for example, 0.375] for a simple fraction [for example, $\frac{3}{8}$] - recall and use equivalences between simple fractions, decimals and percentages, including in different contexts
			Spring 3 Spring 4 Summer 1	Spring 3	Spring 3 Spring 4

Ratio and proportion

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
					• solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts • solve problems involving the calculation/use of percentages for comparison • solve problems involving similar shapes where the scale factor is known or can be found • solve problems involving unequal sharing and grouping using knowledge of fractions and multiples
					Spring 1

Algebra

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
• solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as $7 = \square - 9$	• recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems	• solve problems, including missing number problems			• use simple formulae • generate and describe linear number sequences • express missing number problems algebraically • find pairs of numbers that satisfy an equation with two unknowns • enumerate possibilities of combinations of two variables
					Spring 2

Using measures

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
- compare, describe and solve practical problems for: - lengths and heights - mass/weight - capacity and volume - time - measure and begin to record the following: - lengths and heights - mass/weight - capacity and volume - time (hours, minutes, seconds)	- choose and use appropriate standard units to estimate and measure length/height in any direction (m/cm); mass (kg/g); temperature (°C); capacity (litres/ml) to the nearest appropriate unit, using rulers, scales, thermometers and measuring vessels - compare and order lengths, mass, volume/capacity and record the results using >, < and =	measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)	- Convert between different units of measure [for example, kilometre to metre; hour to minute] - estimate, compare and calculate different measures	- convert between different units of metric measure - understand and use approximate equivalences between metric units and common imperial units such as inches, pounds and pints - use all four operations to solve problems involving measure [for example, length, mass, volume, money] using decimal notation, including scaling	- solve problems involving the calculation and conversion of units of measure, using decimal notation up to 3 d.p. where appropriate - use, read, write and convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation to up to 3 d.p. - convert between miles and kilometres
Spring 4 Spring 5 Summer 6	Spring 3 Spring 4	Spring 2 Spring 4	Spring 2 Summer 3	Spring 4 Summer 5 Summer 6	Autumn 5

Money

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
recognise and know the value of different denominations of coins and notes	- recognise and use symbols for pounds (£) and pence (p); combine amounts to make a particular value - find different combinations of coins that equal the same amounts of money - solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change	add and subtract amounts of money to give change, using both £ and p in practical contexts	estimate, compare and calculate different measures, including money in pounds and pence	use all four operations to solve problems involving measure [for example, money]	
Summer 5	Spring 1	Summer 2	Summer 2	Summer 3	

Time

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
- sequence events in chronological order using language [for example, before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening] - recognise and use language relating to dates, including days of the week, weeks, months and years - tell the time to the hour and half past the hour and draw the hands on a clock face to show these times	- compare and sequence intervals of time - tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times - know the number of minutes in an hour and the number of hours in a day	- tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks - estimate and read time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes and hours; use vocabulary such as o'clock, a.m./p.m., morning, afternoon, noon and midnight - know the number of seconds in a minute and the number of days in each month, year and leap year - compare durations of events [for example to calculate the time taken by particular events or tasks]	- read, write and convert time between analogue and digital 12- and 24-hour clocks - solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days	solve problems involving converting between units of time	use, read, write and convert between standard units, converting measurements of time from a smaller unit of measure to a larger unit, and vice versa Note – In the WRM schemes, time conversions are covered in Y5; the Y6 block concentrates on metric units.
Summer 6	Summer 2	Summer 3	Summer 3	Summer 5	Autumn 5

Perimeter, area, volume

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
		measure the perimeter of simple 2-D shapes	- measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres - find the area of rectilinear shapes by counting squares	- measure and calculate the perimeter of composite rectilinear shapes in centimetres and metres - calculate and compare the area of rectangles (including squares) and including using standard units, square centimetres (cm^2) and square metres (m^2) and estimate the area of irregular shapes - estimate volume [for example, using blocks to build cuboids] and capacity [for example, using water]	- recognise that shapes with the same areas can have different perimeters and vice versa - recognise when it is possible to use formulae for area and volume of shapes - calculate the area of parallelograms and triangles - calculate, estimate and compare volume of cubes and cuboids using standard units, including cubic centimetres (cm^3) and cubic metres (m^3), and extending to other units
		Spring 2	Autumn 3 Spring 2	Spring 4 Summer 6	Spring 5

2-D shapes

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
recognise and name common 2-D shapes [for example, rectangles (including squares), circles and triangles]	- identify and describe the properties of 2-D shapes, including the number of sides and line symmetry in a vertical line - identify 2-D shapes on the surface of 3-D shapes, [for example, a circle on a cylinder and a triangle on a pyramid] - compare and sort common 2-D shapes and everyday objects	draw 2-D shapes	- compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes - identify lines of symmetry in 2-D shapes presented in different orientations	- distinguish between regular and irregular polygons based on reasoning about equal sides and angles. - use the properties of rectangles to deduce related facts and find missing lengths and angles	- draw 2-D shapes using given dimensions and angles - compare and classify geometric shapes based on their properties and sizes - illustrate and name parts of circles, including radius, diameter and circumference and know that the diameter is twice the radius
Autumn 3	Autumn 3	Summer 4	Summer 4	Summer 1	Summer 1

3-D shapes

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
recognise and name common 3-D shapes [for example, cuboids (including cubes), pyramids and spheres]	- recognise and name common 3-D shapes [for example, cuboids (including cubes), pyramids and spheres] - compare and sort common 3-D shapes and everyday objects	make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them		identify 3-D shapes, including cubes and other cuboids, from 2-D representations	recognise, describe and build simple 3-D shapes, including making nets
Autumn 3	Autumn 3	Summer 4		Summer 1	Summer 1

Angles and lines

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
		- recognise angles as a property of shape or a description of a turn - identify right angles, recognise that two right angles make a half-turn, three make three quarters of a turn and four a complete turn; identify whether angles are greater than or less than a right angle - identify horizontal and vertical lines and pairs of perpendicular and parallel lines	- identify acute and obtuse angles and compare and order angles up to two right angles by size - identify lines of symmetry in 2-D shapes presented in different orientations - complete a simple symmetric figure with respect to a specific line of symmetry	- know angles are measured in degrees: estimate and compare acute, obtuse and reflex angles - draw given angles, and measure them in degrees - identify: - angles at a point and one whole turn (total 360°) - angles at a point on a straight line and $\frac{1}{2}$ a turn (total 180°) - other multiples of 90°	- find unknown angles in any triangles, quadrilaterals, and regular polygons - recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles
		Summer 4	Summer 4	Summer 2	Summer 1

Position and direction

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
describe position, direction and movement, including whole, half, quarter and three-quarter turns	- order and arrange combinations of mathematical objects in patterns and sequences - use mathematical vocabulary to describe position, direction and movement, including movement in a straight line and distinguishing between rotation as a turn and in terms of right angles for quarter, half and three-quarter turns (clockwise and anti-clockwise)		- describe positions on a 2-D grid as coordinates in the first quadrant - describe movements between positions as translations of a given unit to the left/right and up/down - plot specified points and draw sides to complete a given polygon	identify, describe and represent the position of a shape following a reflection or translation, using the appropriate language, and know that the shape has not changed	- describe positions on the full coordinate grid (all four quadrants) - draw and translate simple shapes on the coordinate plane, and reflect them in the axes
Summer 3	Summer 4		Summer 6	Summer 2	Summer 2

Present and interpret data

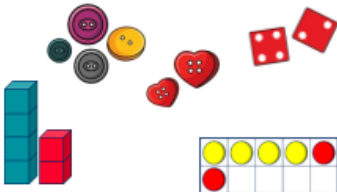
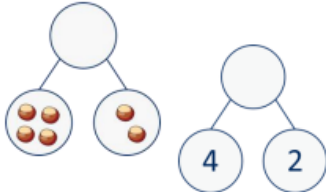
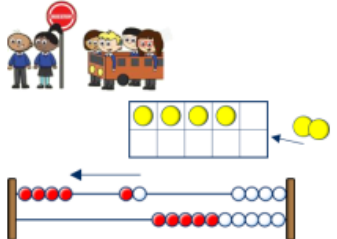
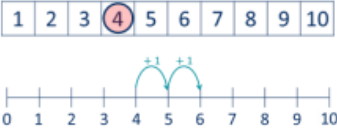
Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
	interpret and construct simple pictograms, tally charts, block diagrams and simple tables	interpret and present data using bar charts, pictograms and tables	interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs	complete, read and interpret information in tables, including timetables	interpret and construct pie charts and line graphs and use these to solve problems
	Summer 3	Summer 5	Summer 5	Spring 5	Spring 6

Solve statistical problems

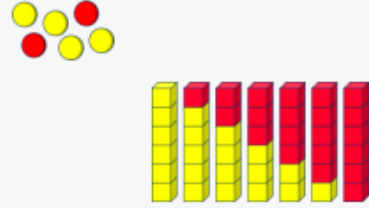
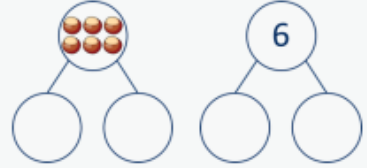
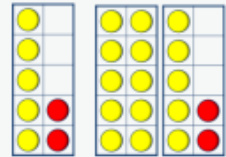
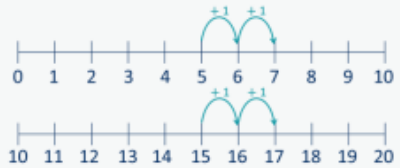
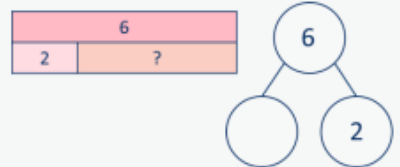
Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
	- ask and answer simple questions by counting the number of objects in each category and sorting the categories by quantity - ask and answer questions about totalling and comparing categorical data	solve one-step and two-step questions [for example, 'How many more?' and 'How many fewer?'] using information presented in scaled bar charts and pictograms and tables	solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs	solve comparison, sum and difference problems using information presented in a line graph	calculate and interpret the mean as an average
	Summer 3	Summer 5	Summer 5	Spring 5	Spring 6

Calculation Policy

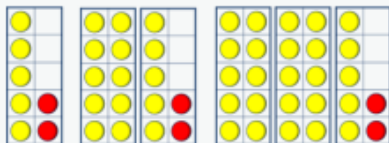
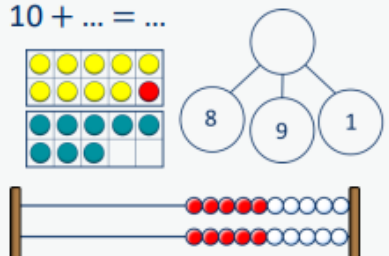
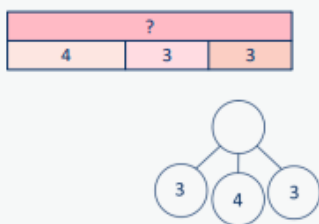
Addition

Year 1	- Read, write and interpret mathematical statements involving addition (+) and equals (=) signs. - Represent and use number bonds within 20 - Add 1-digit and 2-digit numbers to 20, including zero. - Solve one-step problems that involve addition, using concrete objects and pictorial representations, and missing number problems such as $7 = \square + 2$		
Progression of skills	Key representations		
Add together (aggregation) 2 quantities are combined to find the total.	There are ... There are ... There are ... altogether. 	... is a part. ... is a part. ... is the whole. 	... plus ... is equal to is equal to ... + ... $4 + 2 = 6$ $2 + 4 = 6$ $6 = 4 + 2$ $6 = 2 + 4$
Add more (augmentation) A quantity is increased.	First... Then... Now... 	I start at ... I jump on ... I land on ... 	... plus ... is equal to is equal to ... + ... $4 + 2 = 6$ $2 + 4 = 6$ $6 = 4 + 2$ $6 = 2 + 4$

Addition

Progression of skills	Key representations		
Bonds within 10 Include bonds for each number within 10 Encourage children to notice patterns.	... is made of ... and and ... make ... 	... can be partitioned into ... and ... 	... plus ... is equal to ... $6 + 0 = 6$ $5 + 1 = 6$ $4 + 2 = 6$ $3 + 3 = 6$ $2 + 4 = 6$ $1 + 5 = 6$ $0 + 6 = 6$
Related facts within 20 Make links to known facts.	I know that ... and ... = ... so ... and ... = ... 	... more than ... is ... so ... more than ... is ... 	What patterns do you notice? $5 + 2 = 7$ $15 + 2 = 17$ $7 = 5 + 2$ $17 = 15 + 2$
Missing numbers Make links to known facts.	How many more do you need to make ...? 	If ... is the whole and ... is a part, the other part must be... 	... plus ... is equal to ... $2 + \square = 6$ $6 = 2 + \square$ 

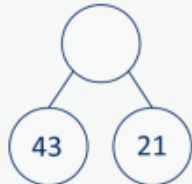
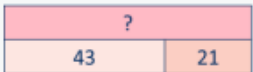
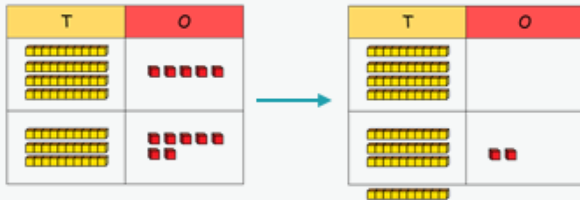
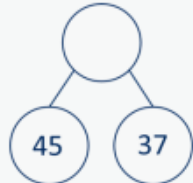
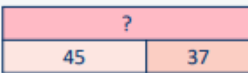
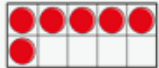
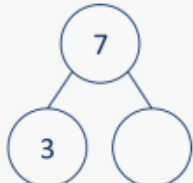
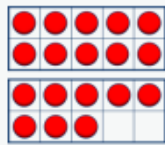
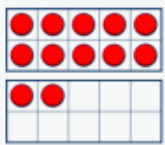
Addition

Year 2	- Recall and use addition facts to 20 fluently, and derive and use related facts up to 100 - Add numbers using concrete objects, pictorial representations, and mentally, including: - a two-digit number and 1s - a two-digit number and 10s 2 two-digit numbers - adding 3 one-digit numbers - Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.		
Progression of skills	Key representations		
Add ones to any number (related facts) Make links to known facts.	I know that ... and ... = ... so ... and ... = ... 	... more than ... is ... so ... more than ... is ... 	What do you notice? Can you continue the pattern? $5 + 2 = 7$ $15 + 2 = 17$ $25 + 2 = 27...$
Add three 1-digit numbers Prompt children to understand that addition can be done in any order and to make links to known facts.	... and ... are a bond to 10 $10 + ... = ...$ 	Double ... + ... = ... 	What do you notice? Which addition is the easiest to calculate? $8 + 9 + 1 =$ $8 + 1 + 9 =$ $9 + 1 + 8 =$

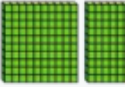
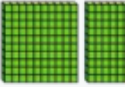
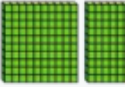
Addition

Progression of skills	Key representations	
Add across a 10 Partition the number being added to make a full ten.	... can be partitioned into ... and ... 8 + 5 = 13 28 + 5 = 33	I add ... to get to ... then I add ...
Add multiples of 10 Make links to known facts within ten.	... ones + ... ones = ... ones so ... tens + ... tens = ... tens 3 + 2 = 5 30 + 20 = 50	What is the same? What is different?
Add 10s to any number Make links to known facts.	... tens + ... tens = ... tens ... tens and ... ones = ...	To add ... I need to add 10 ... times. I know that ... and ... = ... so ... and ... = ... 30 + 20 = 50 34 + 20 = 54

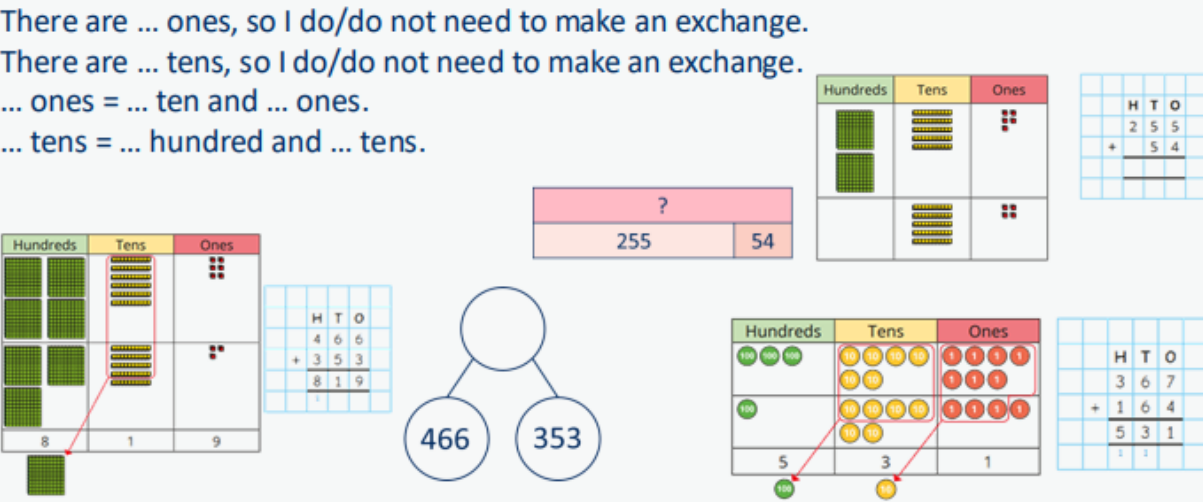
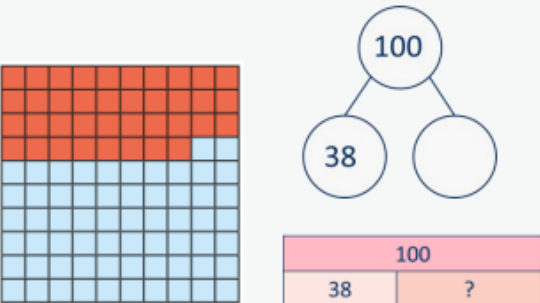
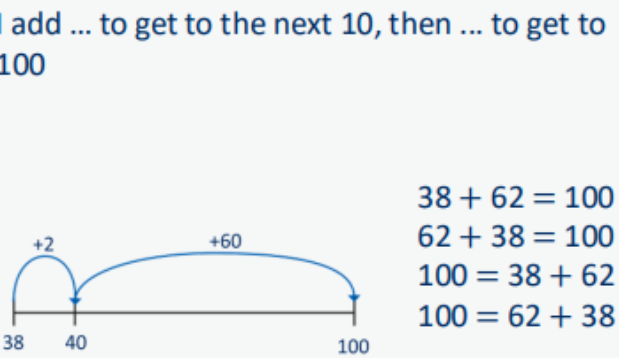
Addition

Progression of skills	Key representations		
Add 2-digit numbers (not across a ten) Lining up ones and tens in columns will support with later written methods.	... ones + ... ones = ... ones ... tens + ... tens = ... tens   3 ones + 1 one = 4 ones 4 tens + 2 tens = 6 tens 6 tens + 4 ones = 64 		
Add 2-digit numbers (across a ten) Begin to exchange 10 ones for 1 ten.	There are ones, so I do/do not need to make an exchange. ... ones = ... ten and ... ones   5 ones + 7 ones = 12 ones 12 ones = 1 ten and 2 ones 4 tens + 3 tens + 1 ten = 8 tens 8 tens and 2 ones = 82 		
Missing numbers Solve missing number problems and use the inverse to check.	How many more do you need to make ...?  $6 + \square = 10$ $10 - \square = 6$	If ... is a whole and ... is a part, then ... is the other part. $\square + 3 = 7$ $7 - 3 = \square$ 	... can be partitioned into ... and ... $10 + 8 = 12 + \square$  

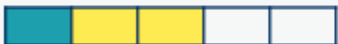
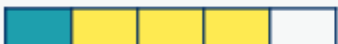
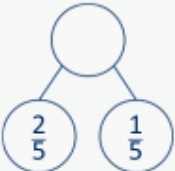
Addition

Year 3	• Add numbers mentally, including: a three-digit number and ones, a three-digit number and tens, a three-digit number and hundreds. • Add numbers with up to three digits, using formal written methods of columnar addition. • Add fractions with the same denominator within 1 whole. • Calculate the time taken by particular events or tasks.																																									
Progression of skills	Key representations																																									
Add 1s, 10s or 100s to a 3-digit number Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.	The ones/tens/hundreds column will increase by ... <table><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td><td></td></tr></table> $444 + 5 =$ $444 + 50 =$ $444 + 500 =$	Hundreds	Tens	Ones				<table><tr><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td></td><td></td></tr></table> $777 + 2 =$ $777 + 20 =$ $777 + 200 =$	H	T	O				What patterns do you notice? $235 + 3 =$ $235 + 30 =$ $235 + 300 =$ $111 + \square = 118$ $111 + \square = 181$ $111 + \square = 811$																											
Hundreds	Tens	Ones																																								
																																										
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Add two numbers (no exchange) Mental strategies and introduction of formal written method.	... ones + ... ones = ... ones ... tens + ... tens = ... tens ... hundreds + ... hundreds = ... hundreds <table><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr></table>  <table><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr></table> <table><tr><th colspan="3">?</th></tr><tr><td>345</td><td></td><td>432</td></tr></table> <table><tr><th>H</th><th>T</th><th>O</th></tr><tr><td>3</td><td>4</td><td>5</td></tr><tr><td>+</td><td>4</td><td>3</td></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr></table>			Hundreds	Tens	Ones							Hundreds	Tens	Ones							?			345		432	H	T	O	3	4	5	+	4	3						
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Addition

Progression of skills	Key representations	
Add two numbers across a 10 or 100 Formal written method involving up to 2 exchanges including 3-digit plus 2-digit numbers.	There are ... ones, so I do/do not need to make an exchange. There are ... tens, so I do/do not need to make an exchange. ... ones = ... ten and ... ones. ... tens = ... hundred and ... tens. 	
Complements to 100 Pairs of numbers which total 100	... plus ... is equal to 100 	I add ... to get to the next 10, then ... to get to 100 

Addition

Progression of skills	Key representations
Add fractions with the same denominator within 1 whole Make links with known facts.	When adding fractions with the same denominator, I only add the numerator. ... fifths + ... fifths = ... fifths  $\frac{1}{5} + \frac{1}{5}$  $\frac{1}{5} + \frac{2}{5}$  $\frac{1}{5} + \frac{3}{5}$  

Addition

Year 4	- Add numbers with up to 4 digits using a formal written method. - Solve simple measure and money problems involving fractions and decimals to 2 decimal places. - Add fractions with the same denominator.	
Progression of skills	Key representations	
Add 1s, 10s and 100s to a 4-digit number Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.	The ones/tens/hundreds/thousands column will increase by ...  $3,425 + 3 =$ $3,425 + 300 =$ $3,425 + 30 =$ $3,425 + 3,000 =$	What patterns do you notice? $2,350 + 3 =$ $2,350 + 30 =$ $2,350 + 300 =$ $2,350 + 3,000 =$ $6,040 + 200 =$ $2,211 + \square = 2,251$ $6,040 + 500 =$ $2,211 + \square = 2,215$ $6,040 + 900 =$ $2,211 + \square = 2,511$
Add up to two 4-digit numbers Formal written method with up to 3 exchanges. Encourage children to estimate and use inverse operations to check answers to calculations.	There are ... ones/tens/hundreds so I do/do not need to make an exchange. I can exchange 10 ... for 1 ...	 

Addition

Progression of skills	Key representations	
Add decimal numbers in the context of money Emphasis on partitioning and use of number lines rather than formal written calculations.	... pence + ... pence = ... pence ... pounds + ... pounds = ... pounds $45\text{p} + 25\text{p} = 70\text{p}$ $\text{£}2 + \text{£}3 = \text{£}5$ $\text{£}5 + 70\text{p} = \text{£}5.70$	$\text{£}3.25$ can be partitioned into $\text{£}3 + 20\text{p} + 5\text{p}$
Add fractions and mixed numbers with the same denominator beyond 1 whole	When adding fractions with the same denominator, I only add the numerator. ... fifths + ... fifths = ... fifths	

Addition

Year 5

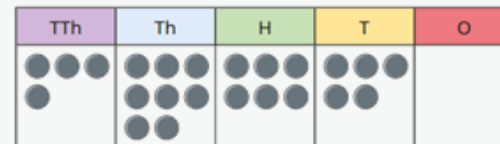
- Add whole numbers with more than 4 digits, including using formal written methods.
- Add numbers mentally with increasingly large numbers.
- Add decimals, including a mix of whole numbers and decimals, decimals with different numbers of decimal places, and complements of 1
- Add fractions with the same denominator, and denominators that are multiples of the same number.

Progression of skills

Key representations

Add using mental strategies

Add 1s, 10s, 100s, etc. to any number.
Use number bonds and related facts.



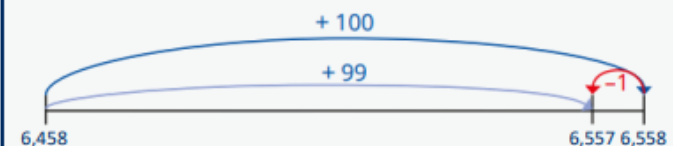
$$48,650 + 300 =$$

$$48,650 + 30,000 =$$

$$48,650 + 30 =$$

To add ..., I can add ... then subtract ...

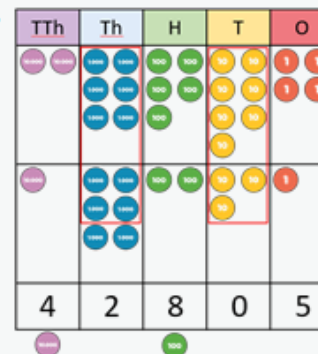
?
6,458 99



Add whole numbers with more than 4 digits

Encourage children to estimate and use inverse operations to check answers to calculations.

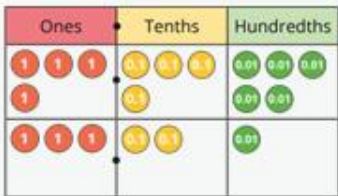
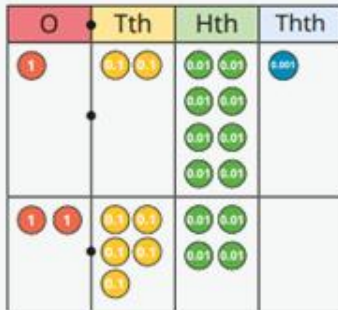
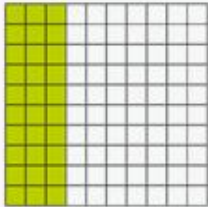
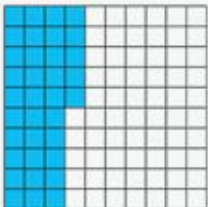
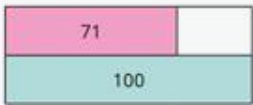
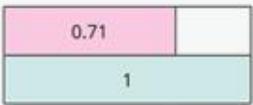
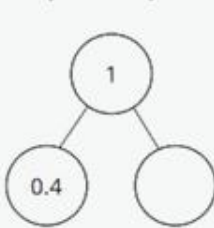
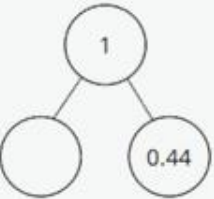
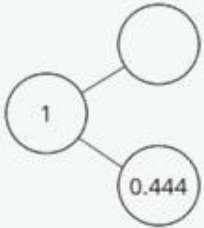
I can exchange 10 ... for 1 ...



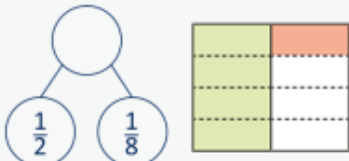
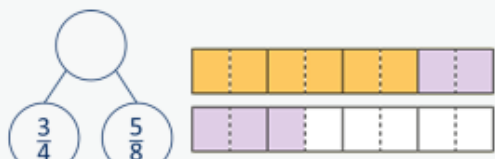
	2	6	5	7	4
+	1	6	2	3	1
	4	2	8	0	5
	1		1		

			4		1	
+	2		8		4	
	8	9	9	2	6	

Addition

Progression of skills	Key representations
Add decimals with up to 2 decimal places Progress from the same number of decimal places to a different number of decimal places, and from no exchange to exchange.	I do/do not need to make an exchange because ... I can exchange 10 ... for 1 ...    
Complements to 1 Pairs of numbers with up to 3 decimal places which total 1 Encourage children to make links with bonds to 10 and complements to 100 and 1,000	$0.3 + \square = 1$  $0.35 + \square = 1$       $4 + 6 = 10$ $44 + 56 = 100$ $444 + 556 = 1,000$ $0.4 + 0.6 = 1$ $0.44 + 0.56 = 1$ $0.444 + 0.556 = 1$

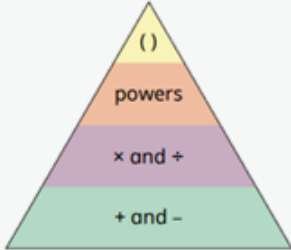
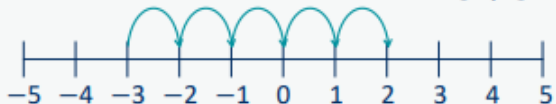
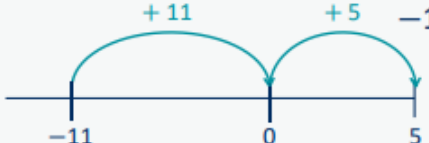
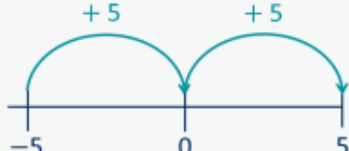
Addition

Progression of skills	Key representations
Add fractions with denominators that are a multiple of one another Encourage children to convert fractions to the same denominator before adding. Progress from adding fractions within 1 whole to adding fractions beyond 1 whole.	The denominator has been multiplied by ..., so the numerator needs to be multiplied by... for the fractions to be equivalent.  $\frac{1}{2} + \frac{1}{8} = \frac{4}{8} + \frac{1}{8} = \frac{5}{8}$  $\frac{3}{4} + \frac{5}{8} = \frac{6}{8} + \frac{5}{8} = \frac{11}{8} = 1\frac{3}{8}$

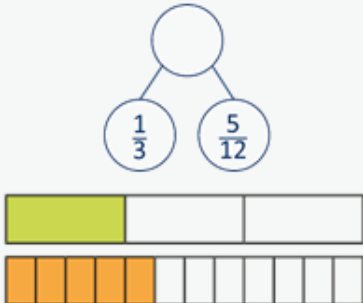
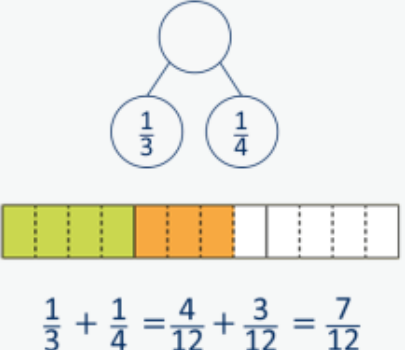
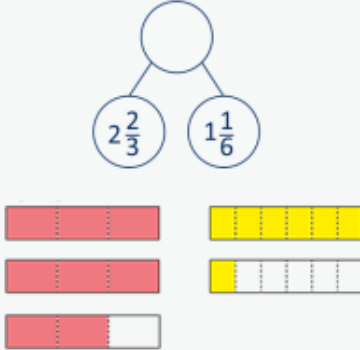
Addition

Year 6	• Add larger numbers, using the formal written method of columnar addition. • Use their knowledge of the order of operations to carry out calculations involving the 4 operations. • Calculate intervals across zero. • Add fractions with different denominators and mixed numbers, using the concept of equivalent fractions.																																																																														
Progression of skills	Key representations																																																																														
Add integers up to 10 million Encourage children to estimate and use inverse operations to check answers to calculations.	<table><tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>3</td><td>4</td><td>6</td><td>2</td><td>2</td><td>1</td></tr><tr><td></td><td>+</td><td>1</td><td>8</td><td>4</td><td>3</td><td>2</td><td>1</td></tr><tr><td></td><td></td><td>5</td><td>3</td><td>0</td><td>5</td><td>4</td><td>2</td></tr><tr><td></td><td></td><td>1</td><td>1</td><td></td><td></td><td></td><td></td></tr></table> <table><tr><td colspan="3">?</td></tr><tr><td>2,354</td><td>750</td><td>1,500</td></tr></table> <table><tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>8</td><td>1</td><td></td><td>8</td><td>5</td><td></td></tr><tr><td></td><td>+</td><td></td><td></td><td>0</td><td>6</td><td></td><td></td></tr><tr><td></td><td></td><td>9</td><td>9</td><td>5</td><td></td><td>8</td><td></td></tr></table>											3	4	6	2	2	1		+	1	8	4	3	2	1			5	3	0	5	4	2			1	1					?			2,354	750	1,500											8	1		8	5			+			0	6					9	9	5		8	
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Add decimals with up to 3 decimal places Progress to numbers with digits in different place value columns. Encourage children to check that they have lined up the columns correctly.	I do/do not need to make an exchange because ... <table><tr><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>3</td><td>1</td><td>0</td><td>8</td></tr><tr><td></td><td>+</td><td>2</td><td>1</td><td>5</td><td>4</td></tr><tr><td></td><td></td><td>5</td><td>2</td><td>6</td><td>2</td></tr><tr><td></td><td></td><td></td><td></td><td>1</td><td></td></tr></table> <table><tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>1</td><td>5</td><td>0</td><td>2</td><td>7</td><td></td></tr><tr><td></td><td>+</td><td>9</td><td>5</td><td>8</td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>2</td><td>4</td><td>6</td><td>0</td><td>7</td><td></td></tr><tr><td></td><td></td><td>1</td><td>1</td><td></td><td></td><td></td><td></td></tr></table>									3	1	0	8		+	2	1	5	4			5	2	6	2					1												1	5	0	2	7			+	9	5	8						2	4	6	0	7				1	1												
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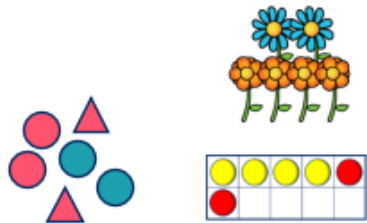
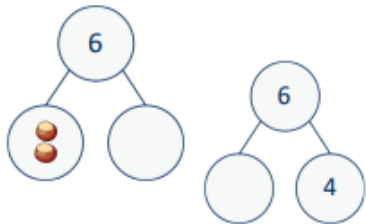
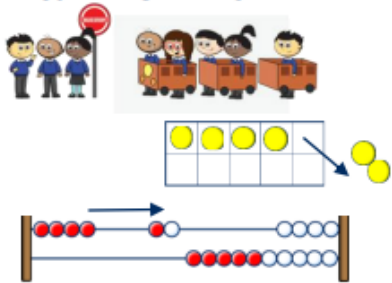
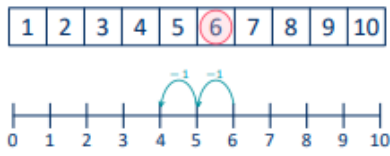
Addition

Progression of skills	Key representations	
Order of operations Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction. *When no brackets are shown and the operations have the same priority, work left to right.	... has greater priority than ..., so the first part of the calculation I need to do is ...   $(3 + 4) \times 2 = 14$  $3 + 4 \times 2 = 11$  $3 \times 4 + 2 = 14$	
Negative numbers Children add to negative numbers and carry out calculations which cross 0	... plus ... is equal to ...  $-3 + 5 = 2$  The difference between -5 and -1 is 4  $-11 + 16 = 5$  The difference between -5 and 5 is 10	

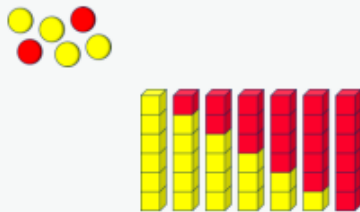
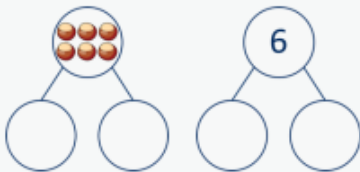
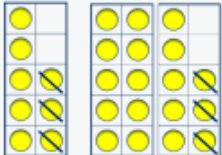
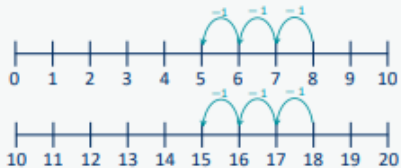
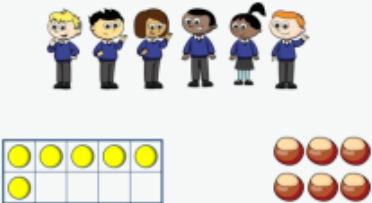
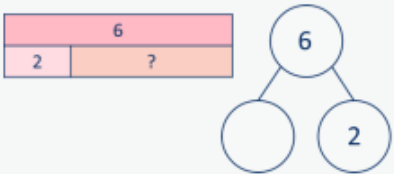
Addition

Progression of skills	Key representations		
Add fractions Convert fractions to the same denominator before adding. Progress from fractions where one denominator is a multiple of the other, to any fractions and then to mixed numbers.	The denominator has been multiplied by ..., so the numerator needs to be multiplied by ... 	The lowest common multiple of ... and ... is ...  $\frac{1}{3} + \frac{1}{4} = \frac{4}{12} + \frac{3}{12} = \frac{7}{12}$	...is made up of ... wholes and ... 

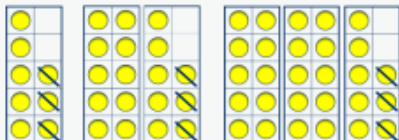
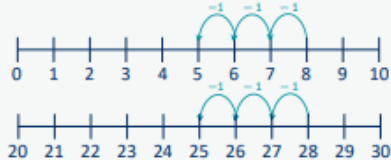
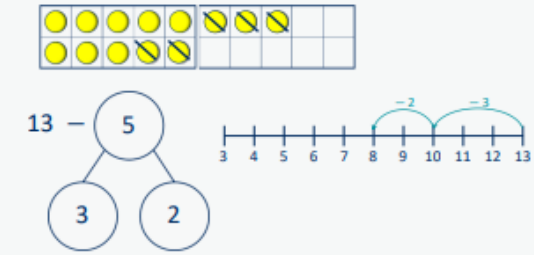
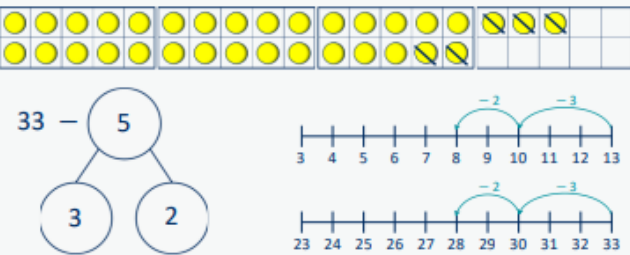
Subtraction

Year 1	- Read, write and interpret mathematical statements involving subtraction (–) and equals (=) signs. - Represent and use number bonds and related subtraction facts within 20 - Subtract one-digit and two-digit numbers to 20, including zero. - Solve one-step problems that involve subtraction, using concrete objects and pictorial representations, and missing number problems such as $7 = \square - 9$		
Progression of skills	Key representations		
Find a part Link to number bonds and known facts. E.g. $2 + 4 = 6$ so if 6 is the whole and 4 is a part, the other part must be 2	There are ... in total. ... are ... How many are not ...? 	... is the whole. ... is a part. ... is a part. 	... subtract ... is equal to is equal to ... – ... $6 - 2 = 4$ $6 - 4 = 2$ $4 = 6 - 2$ $2 = 6 - 4$
Take away A quantity is decreased.	First... Then... Now... 	I start at ... I jump back ... I land on ... 	... minus ... is equal to is equal to ... – ... $6 - 2 = 4$ $6 - 4 = 2$ $4 = 6 - 2$ $2 = 6 - 4$

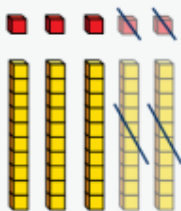
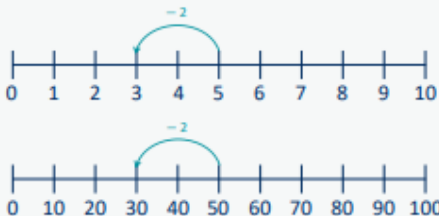
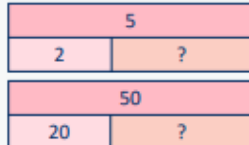
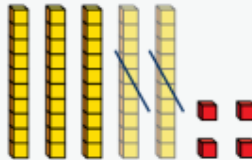
Subtraction

Progression of skills	Key representations		
Bonds within 10 Focus on subtraction facts. Encourage children to notice patterns.	... is made of ... and and ... make ... 	... can be partitioned into ... and ... 	... minus ... is equal to ... $6 - 0 = 6$ $6 - 1 = 5$ $6 - 2 = 4$ $6 - 3 = 3$ $6 - 4 = 2$ $6 - 5 = 1$ $6 - 6 = 0$
Related facts within 20 Make links to known facts.	I know that ... minus ... = ... so ... minus ... = ... 	... less than ... is ... so ... less than ... is ... 	What patterns do you notice? $8 - 3 = 5$ $18 - 3 = 15$ $5 = 8 - 3$ $15 = 18 - 3$
Missing numbers Make links to known facts.	How many do you need to subtract to make ...? 	If ... is the whole and ... is a part, the other part must be... 	... minus ... is equal to ... $6 - \square = 2$ $2 = 6 - \square$ 

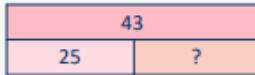
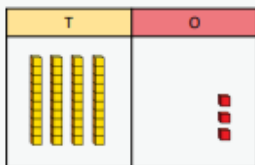
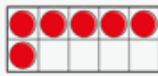
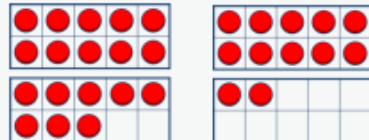
Subtraction

	- Recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100 - Subtract numbers using concrete objects, pictorial representations, and mentally, including: - a two-digit number and 1s - a two-digit number and 10s 2 two-digit numbers - Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.		
Progression of skills	Key representations		
Subtract ones from any number (related facts) Make links to known facts.	I know that ... minus ... = ... so ... minus ... = ... 	... less than ... is ... so ... less than ... is ... 	What do you notice? Can you continue the pattern? $8 - 3 = 5$ $18 - 3 = 15$ $28 - 3 = 25...$
Subtract across a 10 Partition the number being subtracted to bridge through a ten.	... can be partitioned into ... and ... 	Make links with related facts. 	

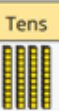
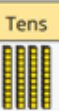
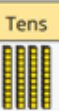
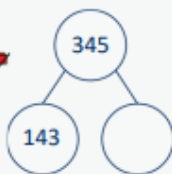
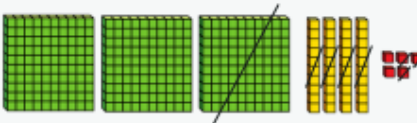
Subtraction

Progression of skills	Key representations																																																														
Subtract multiples of 10 Make links to known facts within ten.	... ones – ... ones = ... ones so ... tens – ... tens = ... tens  $5 - 2 = 3$ $50 - 20 = 30$	What is the same? What is different?   																																																													
Subtract 10s from any number Make links to known facts.	... tens – ... tens = ... tens ... tens and ... ones = ... 	To subtract ... I need to subtract 10 ... times. <table><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr><tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr><tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr><tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr><tr><td>51</td><td>52</td><td>53</td><td>54</td><td>55</td><td>56</td><td>57</td><td>58</td><td>59</td><td>60</td></tr></table>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	I know that ... minus ... = ... so ... minus ... = ... $50 - 20 = 30$ $54 - 20 = 34$
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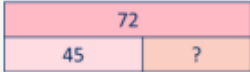
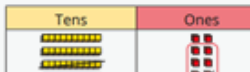
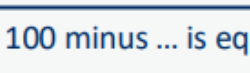
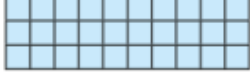
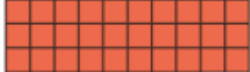
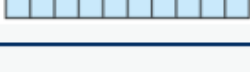
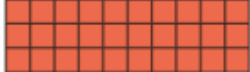
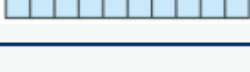
Subtraction

Progression of skills	Key representations		
Subtract two 2-digit numbers (not across a ten)	$\dots \text{ones} - \dots \text{ones} = \dots \text{ones}$ $\dots \text{tens} - \dots \text{tens} = \dots \text{tens}$		$3 \text{ ones} - 1 \text{ one} = 2 \text{ ones}$ $4 \text{ tens} - 2 \text{ tens} = 2 \text{ tens}$ $2 \text{ tens and } 2 \text{ ones} = 22$
Subtract two 2-digit numbers (across a ten) Begin to exchange 1 ten for 10 ones.	I need to make an exchange because I do not have enough ones to subtract $\dots$ ones. 		$3 \text{ ones} - 5 \text{ ones}$ (I need to exchange 1 ten for 10 ones)
Missing numbers Solve missing number problems and use the inverse to check.	How many do you need to subtract to make $\dots$?  $10 - \square = 6$ $6 + \square = 10$	If $\dots$ is a whole and $\dots$ is a part, then $\dots$ is the other part. $7 - 3 = \square$ $\square + 3 = 7$	$\dots$ can be partitioned into $\dots$ and $\dots$ $18 - \square = 12 + 2$ 

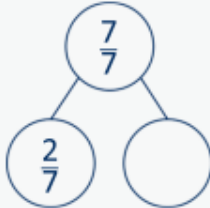
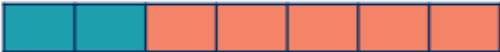
Subtraction

Year 3	- Subtract numbers mentally, including: a three-digit number and ones, a three-digit number and tens, a three-digit number and hundreds. - Subtract numbers with up to three digits, using formal written methods. - Subtract fractions with the same denominator within 1 whole.																																
Progression of skills	Key representations																																
Subtract 1s, 10s and 100s from a 3-digit number Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.	The ones/tens/hundreds column will decrease by ... <table><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td><td></td></tr></table> 444 – 2 = 444 – 20 = 444 – 200 =	Hundreds	Tens	Ones				<table><tr><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td></td><td></td></tr></table> 777 – 4 = 777 – 40 = 777 – 400 =	H	T	O				What patterns do you notice? 235 – 3 = 235 – 30 = 235 – 300 = 118 – = 111 181 – = 111 811 – = 111																		
Hundreds	Tens	Ones																															
																																	
H	T	O																															
																																	
Subtract two numbers (no exchange) Mental strategies and introduction of formal written method.	... ones – ... ones = ... ones ... tens – ... tens = ... tens ... hundreds – ... hundreds = ... hundreds  <table><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr></table> <table><tr><td colspan="3">769</td></tr><tr><td>147</td><td colspan="2">?</td></tr></table> <table><tr><td></td><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td>7</td><td>6</td><td>9</td></tr><tr><td>–</td><td>1</td><td>4</td><td>7</td></tr><tr><td></td><td></td><td></td><td></td></tr></table>		Hundreds	Tens	Ones							769			147	?			H	T	O		7	6	9	–	1	4	7				
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Subtraction

Progression of skills	Key representations
Subtract two numbers across a 10 or 100 Formal written method involving up to 2 exchanges including 3-digit subtract 2-digit numbers.	I need to subtract ... ones. I do/do not need to make an exchange. I need to subtract ... tens. I do/do not need to make an exchange. I can exchange 1 ... for 10 ...       
Complements to 100 Focus on subtraction facts. Encourage children to notice patterns.	100 minus ... is equal to ...   
	I subtract ... tens, then I subtract ... ones.   

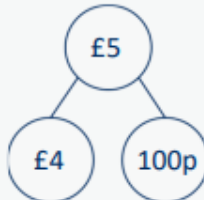
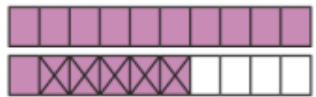
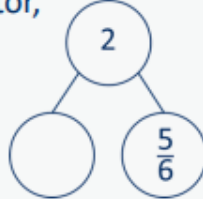
Subtraction

Progression of skills	Key representations
Subtract fractions with the same denominator within 1 whole Make links with known facts.	When subtracting fractions with the same denominator, I only subtract the numerator. ... fifths – ... fifths = ... fifths  $\frac{5}{5} - \frac{1}{5}$  $\frac{4}{5} - \frac{1}{5}$  $\frac{3}{5} - \frac{1}{5}$  

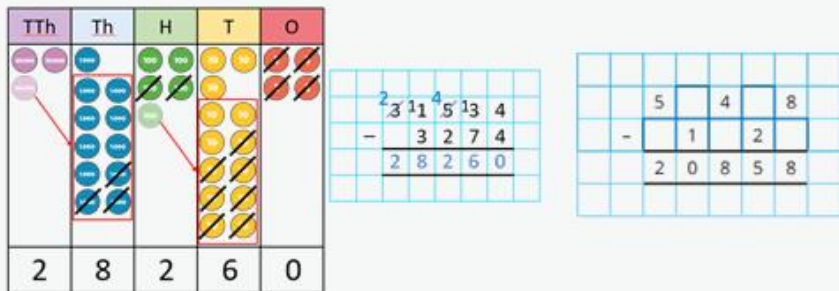
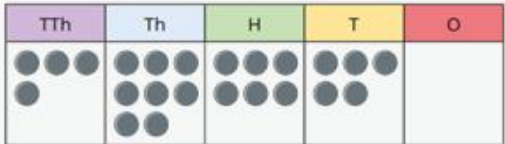
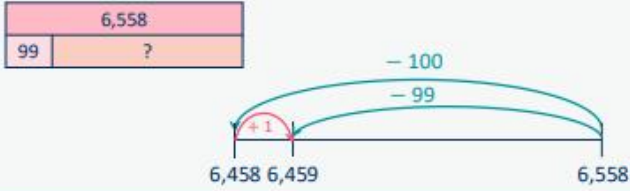
Subtraction

Year 4	- Subtract numbers with up to 4 digits using a formal written method. - Solve simple measure and money problems involving fractions and decimals to 2 decimal places. - Subtract fractions with the same denominator.																														
Progression of skills	Key representations																														
Subtract 1s, 10s, 100s and 1,000s from a 4-digit number Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.	The ones/tens/hundreds/thousands column will decrease by ... <table><tr><th>Thousands</th><th>Hundreds</th><th>Tens</th><th>Ones</th></tr><tr><td> 1,000 1,000 1,000 </td><td> 100 100 100 100 </td><td> 10 10 </td><td> 1 1 1 1 1 </td></tr></table> 3,425 – 2 = 3,425 – 200 = 3,425 – 20 = 3,425 – 2,000 =	Thousands	Hundreds	Tens	Ones	1,000 1,000 1,000	100 100 100 100	10 10	1 1 1 1 1	What patterns do you notice? 4,356 – 3 = 4,356 – 30 = 4,356 – 300 = 4,356 – 3,000 = 4,433 – = 4,430 4,433 – = 4,033 4,433 – = 4,403																					
Thousands	Hundreds	Tens	Ones																												
1,000 1,000 1,000	100 100 100 100	10 10	1 1 1 1 1																												
Subtract up to two 4-digit numbers Formal written method with up to 3 exchanges. Encourage children to estimate and use inverse operations to check answers to calculations.	I need to subtract... ones/tens/hundreds. I do/do not need to make an exchange. I can exchange 1... for 10... <table><tr><th>Th</th><th>H</th><th>T</th><th>O</th></tr><tr><td> 1,000 1,000 1,000 </td><td> 100 </td><td> 10 10 10 10 10 10 10 10 </td><td> 1 </td></tr></table> <table><tr><th>Th</th><th>H</th><th>T</th><th>O</th></tr><tr><td>3</td><td>2</td><td>4</td><td>8</td></tr><tr><td>-</td><td>2</td><td>1</td><td>4</td></tr><tr><td></td><td>1</td><td>0</td><td>5</td></tr><tr><td></td><td></td><td></td><td>8</td></tr></table>			Th	H	T	O	1,000 1,000 1,000	100	10 10 10 10 10 10 10 10	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Th	H	T	O	3	2	4	8	-	2	1	4		1	0	5				8
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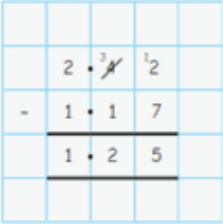
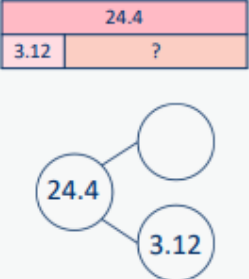
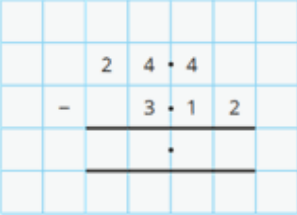
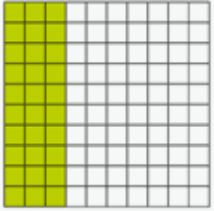
Subtraction

Progression of skills	Key representations	
Subtract decimal numbers in the context of money Emphasis here is on partitioning and use of number lines rather than formal written calculations.	I can partition £... into £... and 100p $£... - £... = £...$ $100p - ...p = ...p$ £5 – £3.26 $£4 - £3 = £1$ $100p - 26p = 74p$ $£5 - £3.26 = £1.74$ 	£3.26 can be partitioned into £3 + 20p + 6p 
Subtract fractions and mixed numbers with the same denominator Include subtracting fractions from wholes.	When subtracting fractions with the same denominator, I only subtract the numerator. ... tenths – ... tenths = ... tenths  $\frac{16}{10} - \frac{5}{10}$  $\frac{16}{10} - \frac{9}{10}$	  

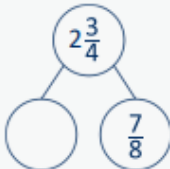
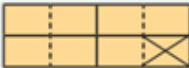
Subtraction

Year 5	- Subtract whole numbers with more than 4 digits. - Subtract numbers mentally with increasingly large numbers. - Subtract decimals, including a mix of whole numbers and decimals, decimals with different numbers of decimal places, and complements of 1 - Subtract fractions with the same denominator, and denominators that are multiples of the same number.	
Progression of skills	Key representations	
Subtract whole numbers with more than 4 digits Encourage children to estimate and use inverse operations to check answers to calculations.	I can exchange 1 ... for 10 ... 	
Subtract using mental strategies Subtract 1s, 10s, 100s etc from any number. Use number bonds and related facts.	 $48,650 - 300 =$ $48,650 - 30,000 =$ $48,650 - 30 =$	To subtract ..., I can subtract ... then add ... 

Subtraction

Progression of skills	Key representations																
Subtract decimals with up to 2 decimal places Progress from the same number of decimal places to a different number of decimal places and from no exchange to exchange.	   																
Complements to 1 Encourage children to make links with bonds to 10 and complements to 100 and 1,000 when finding a missing part or subtracting from 1	 $0.3 + \square = 1$  $0.35 + \square = 1$  <table border="1"> <tr> <td>10</td> <td></td> </tr> <tr> <td>3</td> <td>?</td> </tr> </table> <table border="1"> <tr> <td>100</td> <td></td> </tr> <tr> <td>35</td> <td>?</td> </tr> </table> <table border="1"> <tr> <td>1</td> <td></td> </tr> <tr> <td>0.3</td> <td>?</td> </tr> </table> <table border="1"> <tr> <td>1</td> <td></td> </tr> <tr> <td>0.35</td> <td>?</td> </tr> </table> $10 - 4 = 6$ $1 - 0.4 = 0.6$ $100 - 44 = 56$ $1 - 0.44 = 0.56$ $1,000 - 444 = 556$ $1 - 0.444 = 0.556$	10		3	?	100		35	?	1		0.3	?	1		0.35	?
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Subtraction

Progression of skills	Key representations
Subtract fractions with denominators that are a multiple of one another Convert fractions to the same denominator before subtracting. Progress from subtracting fractions within 1 whole to subtracting from a mixed number.	The denominator has been multiplied by ..., so the numerator needs to be multiplied by... for the fractions to be equivalent.  $\frac{1}{3} - \frac{1}{15} = \frac{5}{15} - \frac{1}{15} = \frac{4}{15}$  $\frac{2}{3} - \frac{2}{9} = \frac{6}{9} - \frac{2}{9} = \frac{4}{9}$    

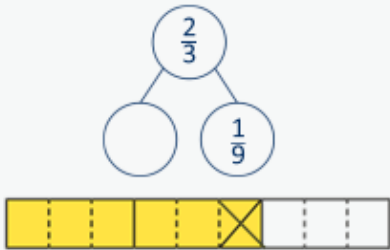
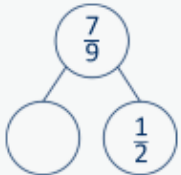
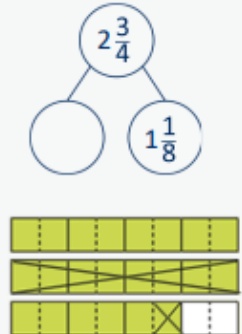
Subtraction

Year 6	- Subtract larger numbers, using the formal written methods of columnar subtraction. - Use their knowledge of the order of operations to carry out calculations involving the 4 operations. - Calculate intervals across zero. - Subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions.																																																																						
Progression of skills	Key representations																																																																						
Subtract integers up to 10 million Encourage children to estimate and use inverse operations to check answers to calculations.	<table><tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>²3</td><td>¹4</td><td>⁵6</td><td>¹2</td><td>2</td><td>1</td></tr><tr><td></td><td>-</td><td>1</td><td>8</td><td>4</td><td>3</td><td>2</td><td>1</td></tr><tr><td></td><td></td><td>1</td><td>6</td><td>1</td><td>9</td><td>0</td><td>0</td></tr></table><table><tr><td colspan="3">4,604</td></tr><tr><td>2,354</td><td>750</td><td>?</td></tr></table><table><tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>8</td><td></td><td>4</td><td>8</td><td>5</td><td></td></tr><tr><td></td><td>-</td><td>3</td><td>6</td><td></td><td></td><td></td><td>4</td></tr><tr><td></td><td></td><td>5</td><td>5</td><td>5</td><td>5</td><td>5</td><td></td></tr></table>											² 3	¹ 4	⁵ 6	¹ 2	2	1		-	1	8	4	3	2	1			1	6	1	9	0	0	4,604			2,354	750	?											8		4	8	5			-	3	6				4			5	5	5	5	5	
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Subtract decimals with up to 3 decimal places Progress from the same number of decimal and whole number places to a different number of decimal and whole number places.	I do/do not need to make an exchange because ... <table><tr><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>6</td><td>⁶7</td><td>¹3</td></tr><tr><td></td><td>-</td><td>1</td><td>3</td><td>4</td></tr><tr><td></td><td></td><td>5</td><td>3</td><td>9</td></tr></table><table><tr><th>O</th><th>Tth</th><th>Hth</th><th>Thth</th></tr><tr><td>0</td><td>9</td><td>7</td><td>5</td></tr></table><table><tr><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>⁰1</td><td>¹⁵6</td><td>¹1</td></tr><tr><td></td><td>-</td><td>0</td><td>6</td><td>4</td></tr><tr><td></td><td></td><td>0</td><td>9</td><td>7</td></tr></table>								6	⁶ 7	¹ 3		-	1	3	4			5	3	9	O	Tth	Hth	Thth	0	9	7	5								⁰ 1	¹⁵ 6	¹ 1		-	0	6	4			0	9	7																						
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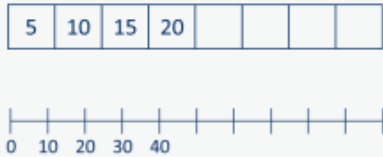
Subtraction

Progression of skills	Key representations
Order of operations Children learn the order of priority for operations in a calculation. Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction.	... has greater priority than ... , so the first part of the calculation I need to do is ... A triangle divided into four horizontal sections. From top to bottom: a yellow section with '()', an orange section with 'powers', a purple section with '× and ÷', and a green section with '+ and -'. Three dot diagrams illustrating calculations. The first shows 8 dots with 2 groups of 2 dots crossed out, representing $8 - 2 \times 3 = 2$. The second shows 8 dots with 2 groups of 2 dots crossed out, representing $(8 - 2) \times 3 = 18$. The third shows 8 dots with 2 groups of 2 dots crossed out, representing $8 - 2^2 = 4$.

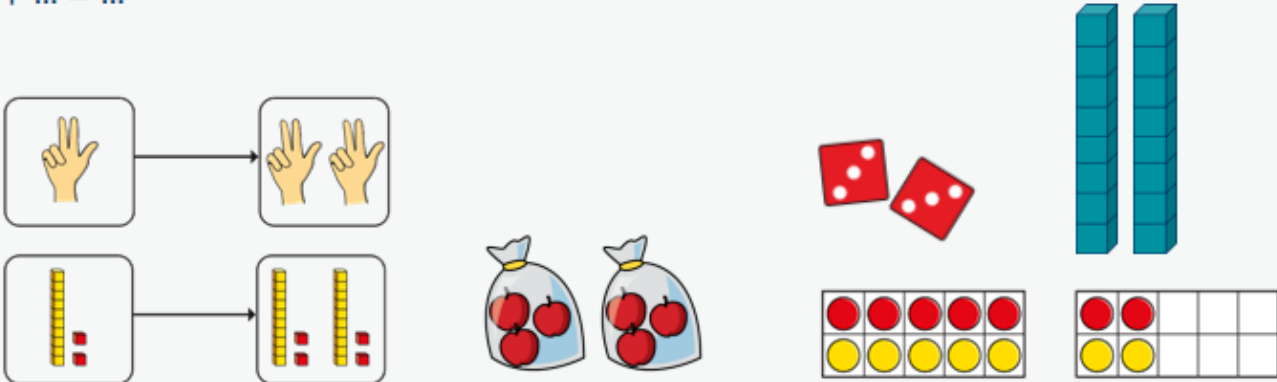
Subtraction

Progression of skills	Key representations		
Subtract fractions Convert fractions to the same denominator before subtracting. Progress from fractions where one denominator is a multiple of the other, to any fractions and then subtracting from a mixed number.	The denominator has been multiplied by ..., so the numerator needs to be multiplied by...  $\frac{2}{3} - \frac{1}{9} = \frac{6}{9} - \frac{1}{9} = \frac{5}{9}$	The lowest common multiple of ... and ... is ...  $\frac{7}{9} - \frac{1}{2} = \frac{14}{18} - \frac{9}{18} = \frac{5}{18}$	... is made up of ... wholes and ...  $2\frac{3}{4} - 1\frac{1}{8} = 1\frac{5}{8}$

Multiplication

Year 1	- Count in multiples of twos, fives and tens. - Solve one-step problems involving multiplication, using concrete objects, pictorial representations and arrays with the support of the teacher.		
Progression of skills	Key representations		
Count in 2s, 5s and 10s Begin by counting objects that naturally come in 2s, 5s and 10s, for example pairs of socks or fingers.	There are ... equal groups of ... There are ... altogether. 	Continue to colour in ...s What do you notice? 	Complete the number track/number line by counting in ...s. 
Add equal groups (repeated addition) Children should be able to write a repeated addition to represent equal groups and to draw pictures or use objects to represent a repeated addition.	There are ... groups of ... There are ... altogether.  $10 + 10 + 10 = 30$ $5 + 5 + 5 + 5 = 20$		What is the same? What is different? $2 + 2 + 2 =$ $5 + 5 + 5 =$ $10 + 10 + 10 =$ Use objects or a drawing to represent the equal groups and find how many in total.

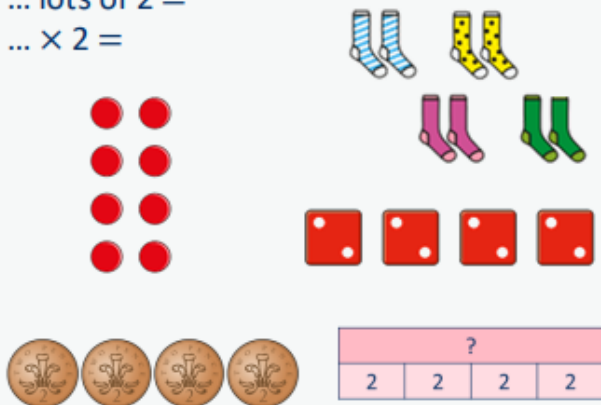
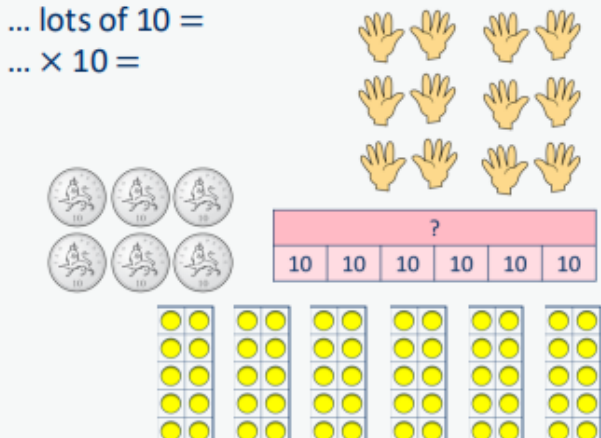
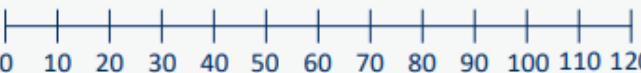
Multiplication

Progression of skills	Key representations
Make arrays Children use their knowledge of adding equal groups to arrange objects in columns and rows.	There are ... rows of ... There are ... altogether. There are ... columns of ... There are ... altogether. 
Make doubles Children understand that doubles are two equal groups. Children may begin to explore doubles beyond 20 using base 10	Double ... is ... $\dots + \dots = \dots$ 

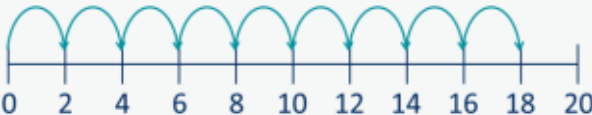
Multiplication

Year 2	- Recall and use multiplication facts for the 2, 5 and 10 multiplication tables. - Calculate mathematical statements for multiplication within the multiplication tables and write them using the multiplication ($\times$) and equals ($=$) signs. - Show that multiplication of two numbers can be done in any order (commutative).													
Progression of skills	Key representations													
Link repeated addition and multiplication	There are ... equal groups with ... in each group. There are ... altogether. <table border="1" data-bbox="1426 644 1610 721"><tr><td colspan="2">6</td></tr><tr><td>3</td><td>3</td></tr></table> $3 + 3 = 6$ $2 \times 3 = 6$ <table border="1" data-bbox="1337 786 1610 863"><tr><td colspan="4">20</td></tr><tr><td>5</td><td>5</td><td>5</td><td>5</td></tr></table> $5 + 5 + 5 + 5 = 20$ $4 \times 5 = 20$		6		3	3	20				5	5	5	5
6														
3	3													
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Use arrays	There are ... rows with ... in each row. There are ... columns with ... in each column.  $3 \text{ lots of } 5 = 15$ $5 + 5 + 5 = 15$ $5 \text{ lots of } 3 = 15$ $3 + 3 + 3 + 3 + 3 = 15$	I can see ... $\times$... and ... $\times$... $3 \times 5 = 15$ $5 \times 3 = 15$ $3 \times 5 = 5 \times 3$												
Double	Double ... is ... $\rightarrow$ $\text{Double } 4 = 4 + 4$ $\text{Double } 4 \text{ is } 8$	Double ... is ... so double ... is ... $\rightarrow$ $\text{Double } 4 \text{ is } 8$ $\rightarrow$ $\text{Double } 40 \text{ is } 80$												

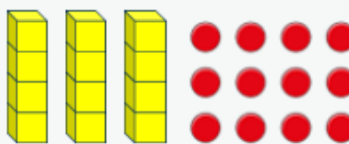
Multiplication

Progression of skills	Key representations																																									
The 2 times-table Encourage daily counting in multiples both forwards and back. Notice that all multiples of 2 are even numbers.	... lots of 2 = ... $\times 2 =$ 	... times 2 is equal to ... <table border="1"><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr><tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr></table> $1 \times 2 = 2$ $2 = 1 \times 2$ $2 \times 2 = 4$ $4 = 2 \times 2$ $3 \times 2 = 6$ $6 = 3 \times 2$ 	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30										
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The 10 times-table Encourage daily counting in multiples both forwards and back. Notice the pattern in the numbers.	... lots of 10 = ... $\times 10 =$ 	... times 10 is equal to ... <table border="1"><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr><tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr><tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr></table> $1 \times 10 = 10$ $10 = 1 \times 10$ $2 \times 10 = 20$ $20 = 2 \times 10$ $3 \times 10 = 30$ $30 = 3 \times 10$ 	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
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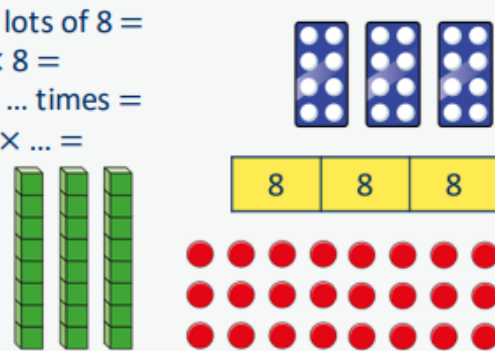
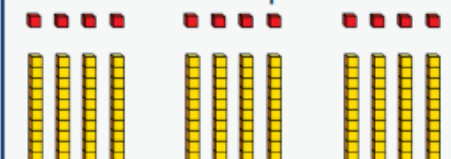
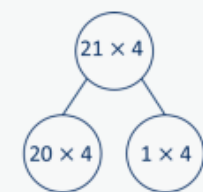
Multiplication

Progression of skills	Key representations																																																			
The 5 times-table Encourage daily counting in multiples both forwards and back. Notice the pattern in the numbers.	... lots of 5 = ... $\times 5 =$    <table border="1"><tr><td colspan="5">?</td></tr><tr><td>5</td><td>5</td><td>5</td><td>5</td><td>5</td></tr></table>	?					5	5	5	5	5	... times 5 is equal to ... <table border="1"><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr><tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr><tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr></table> $1 \times 5 = 5$$5 = 1 \times 5$ $2 \times 5 = 10$$10 = 2 \times 5$ $3 \times 5 = 15$$15 = 3 \times 5$ 	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
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Missing numbers Make links to known facts.	... is equal to ... groups of ... 18 socks, how many pairs?  	... times ... is equal to ... $\square \times 2 = 18$ $18 = 2 \times \square$																																																		

Multiplication

Year 3	- Recall and use multiplication facts for the 3, 4 and 8 multiplication tables. - Write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods. - Solve problems, including missing number problems, involving multiplication, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects.																															
Progression of skills	Key representations																															
The 3 times-table Encourage daily counting in multiples both forwards and back.	... groups of 3 = ... $\times 3 =$ 3, ... times = $3 \times \dots =$  	... times 3 is equal to ... <table border="1" data-bbox="1397 772 1823 900"><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr><tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr></table> $4 \times 3 = 12$ $12 = 4 \times 3$ 	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
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11	12	13	14	15	16	17	18	19	20																							
21	22	23	24	25	26	27	28	29	30																							
The 4 times-table Encourage daily counting in multiples both forwards and back. Encourage children to notice links between the 2 and 4 times-tables.	... groups of 4 = ... $\times 4 =$ 4, ... times = $4 \times \dots =$  	... times 4 is equal to ... <table border="1" data-bbox="1397 1099 1823 1227"><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr><tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr></table> $3 \times 4 = 12$ $12 = 3 \times 4$ 	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
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Multiplication

Progression of skills	Key representations																															
The 8 times-table Encourage daily counting in multiples both forwards and back. Encourage children to notice links between the 2, 4 and 8 times-tables.	... lots of 8 = $\times 8 =$ 8, ... times = $8 \times \dots =$ 	... times 8 is equal to ... <table border="1"><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr><tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr></table> $3 \times 8 = 24$ $24 = 3 \times 8$ 	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
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Related facts Use knowledge of multiplying by 10 to scale times-table facts.	... $\times$... ones is equal to ... ones so ... $\times$... tens is equal to ... tens.  	$3 \times 4 = 12$ $3 \times 40 = 120$																														
Multiply a 2-digit number by a 1-digit number - no exchange Children apply their understanding of partitioning to represent and solve calculations using the expanded method.	... tens multiplied by ... is equal to ... tens. ...ones multiplied by ... is equal to ... ones. <table border="1"><thead><tr><th>Tens</th><th>Ones</th></tr></thead><tbody><tr><td></td><td></td></tr><tr><td></td><td></td></tr></tbody></table> $30 \times 2 = 60$ $2 \times 2 = 4$ $32 \times 2 = 64$	Tens	Ones					 <table border="1"><thead><tr><th>Tens</th><th>Ones</th></tr></thead><tbody><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></tbody></table>	Tens	Ones																						
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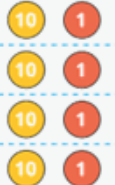
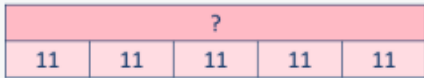
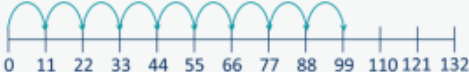
Multiplication

Progression of skills	Key representations																									
Multiply a 2-digit number by a 1-digit number - with exchange Children apply their understanding of partitioning to represent and solve calculations using the expanded method.	... tens multiplied by ... is equal to ... tens. ... ones multiplied by ... is equal to ... ones. <table><tr><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table> $20 \times 4 = 80$ $4 \times 4 = 16$ $24 \times 4 = 96$	Tens	Ones													<pre>graph TD; A((45 x 3)) --- B((40 x 3)); A --- C((5 x 3))</pre> <table><tr><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table>	Tens	Ones								
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Scaling Children focus on multiplication as scaling (... times the size) as opposed to repeated addition.	There are times as many ... as ... 2 22 There are 3 times as many triangles as circles.	... is ... times the size of is ... times the length/height of ... 4 cm16 cm Miss Smith is twice the height of Jo.																								

Multiplication

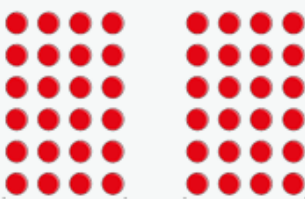
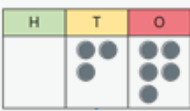
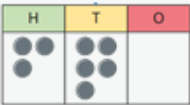
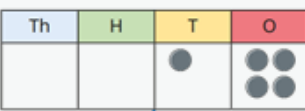
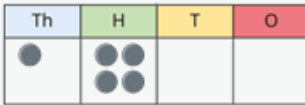
Progression of skills	Key representations								
Correspondence problems (How many ways?) Encourage children to work systematically to find all the different possible combinations.	For every ... , there are ... possible ... There are ... $\times$... possibilities altogether.  <table border="1" data-bbox="1086 526 1366 861"> <thead> <tr> <th>hats</th><th>scarves</th></tr> </thead> <tbody> <tr> <td>blue </td><td> </td></tr> <tr> <td>orange </td><td> </td></tr> <tr> <td>purple </td><td> </td></tr> </tbody> </table> For every hat, there are two possible scarves. $3 \times 2 = 6$ There are 6 possibilities altogether.	hats	scarves	blue 	 	orange 	 	purple 	 
hats	scarves								
blue 	 								
orange 	 								
purple 	 								

Multiplication

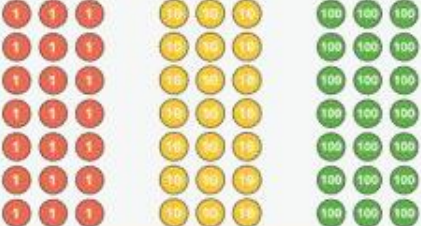
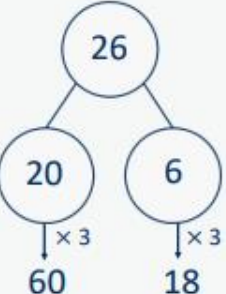
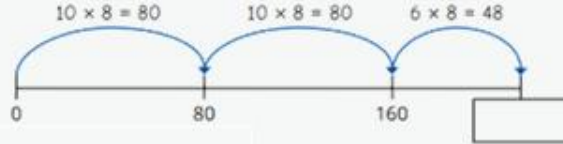
Year 4	- Recall multiplication facts for multiplication tables up to 12×12 - Use place value, known and derived facts to multiply mentally, including: multiplying by 0 and 1; multiplying together three numbers. - Recognise and use factor pairs and commutativity in mental calculations. - Multiply two-digit and three-digit numbers by a one-digit number using formal written layout. - Solve problems involving multiplying and adding, including using the distributive law to multiply two-digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects.																																																																																																					
Progression of skills	Key representations																																																																																																					
Times-table facts to 12×12 Encourage daily counting in multiples both forwards and back. Encourage children to notice links between related times-tables.	... groups of ... = ... times ... is equal to $\times$... =    <table border="1" data-bbox="1597 807 1883 1082"><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr><tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr><tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr><tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr><tr><td>51</td><td>52</td><td>53</td><td>54</td><td>55</td><td>56</td><td>57</td><td>58</td><td>59</td><td>60</td></tr><tr><td>61</td><td>62</td><td>63</td><td>64</td><td>65</td><td>66</td><td>67</td><td>68</td><td>69</td><td>70</td></tr><tr><td>71</td><td>72</td><td>73</td><td>74</td><td>75</td><td>76</td><td>77</td><td>78</td><td>79</td><td>80</td></tr><tr><td>81</td><td>82</td><td>83</td><td>84</td><td>85</td><td>86</td><td>87</td><td>88</td><td>89</td><td>90</td></tr><tr><td>91</td><td>92</td><td>93</td><td>94</td><td>95</td><td>96</td><td>97</td><td>98</td><td>99</td><td>100</td></tr></table>		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
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Multiply by 1 and 0	Any number multiplied by 1 is equal to ... Any number multiplied by 0 is equal to ...  	... $\times$... = ... <table><tr><td>$1 \times 1 = 1$</td><td>$1 \times 0 = 0$</td></tr><tr><td>$2 \times 1 = 2$</td><td>$2 \times 0 = 0$</td></tr><tr><td>$3 \times 1 = 3$</td><td>$3 \times 0 = 0$</td></tr><tr><td>$4 \times 1 = 4$</td><td>$4 \times 0 = 0$</td></tr></table>	$1 \times 1 = 1$	$1 \times 0 = 0$	$2 \times 1 = 2$	$2 \times 0 = 0$	$3 \times 1 = 3$	$3 \times 0 = 0$	$4 \times 1 = 4$	$4 \times 0 = 0$																																																																																												
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61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
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91	92	93	94	95	96	97	98	99	100

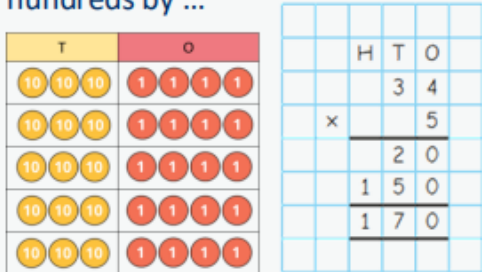
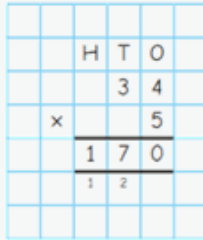
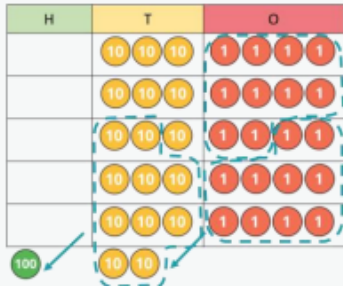
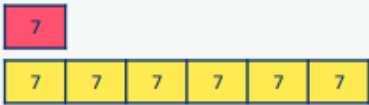
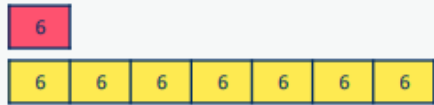
Multiplication

Progression of skills	Key representations	
Multiply 3 numbers Children use their understanding of commutativity to multiply more efficiently.	To work out ... $\times$... $\times$..., I can first calculate ... $\times$... and then multiply the answer by ...  $4 \times 2 \times 3 = 8 \times 3 = 24$ $2 \times 3 \times 4 = 6 \times 4 = 24$ $3 \times 4 \times 2 = 12 \times 2 = 24$	
Factor pairs Children explore equivalent calculations using different factors pairs.	$12 = \dots \times \dots$, so ... $\times 12 = \dots \times \dots \times \dots$  $8 \times 6 = 8 \times 3 \times 2$ $8 \times 6 = 24 \times 2$  $6 \times 8 = 6 \times 4 \times 2$ $6 \times 8 = 24 \times 2$	
Multiply by 10 and 100 Some children may over-generalise that multiplying by 10 or 100 always results in adding zeros. This will cause issues later when multiplying decimals.	When I multiply by 10, the digits move ... place value column to the left. ... is 10 times the size of ...   $35 \times 10 = 350$	When I multiply by 100, the digits move ... place value columns to the left. ... is 100 times the size of ...   $14 \times 100 = 1,400$

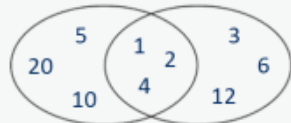
Multiplication

Progression of skills	Key representations								
Related facts Use knowledge of multiplying by 10 and 100 to scale times-table facts.	... $\times$... ones is equal to ... ones so ... $\times$... tens is equal to ... tens and ... $\times$... hundreds is equal to ... hundreds.  $3 \times 7 = 21$ $3 \times 70 = 210$ $3 \times 700 = 2,100$ $7 \times 3 = 21$ $7 \times 30 = 210$ $7 \times 300 = 2,100$								
Mental strategies Partition 2 or 3-digit numbers to multiply using informal methods.	... tens multiplied by ... is equal to ... tens. ...ones multiplied by ... is equal to ... ones. <table border="1" data-bbox="689 941 996 1189"> <thead> <tr> <th>Tens</th><th>Ones</th></tr> </thead> <tbody> <tr> <td></td><td></td></tr> <tr> <td></td><td></td></tr> <tr> <td></td><td></td></tr> </tbody> </table>  $3 \times 26 = 60 + 18 = 78$  $26 \times 8 = 80 + 80 + 48 = 208$	Tens	Ones						
Tens	Ones								

Multiplication

Progression of skills	Key representations																								
Multiply a 2 or 3-digit number by a 1-digit number The short multiplication method is introduced for the first time, initially in an expanded form.	To multiply a 2-digit number by ..., I multiply the ones by ... and the tens by ... To multiply a 3-digit number by ..., I multiply the ones by ..., the tens by ... and the hundreds by ...   (4 × 5) (30 × 5) 																								
Scaling Children focus on multiplication as scaling (... times the size).	... is ... times the size of ...  A computer mouse costs £7 A keyboard costs 6 times as much.  A red ribbon is 6 cm. A yellow ribbon is 7 times as long.																								
Correspondence problems Encourage children to use tables to show all the different possible combinations.	For every ..., there are ... possibilities. There are ... × ... possibilities altogether. A pizza company offers a choice of 5 toppings and 3 bases. $5 \times 3 = 15$ <table border="1"> <thead> <tr> <th></th><th>Deep pan</th><th>Italian</th><th>Thin</th></tr> </thead> <tbody> <tr> <td>Cheese</td><td>C DP</td><td>C I</td><td>C Th</td></tr> <tr> <td>Mushroom</td><td>M DP</td><td>M I</td><td>M Th</td></tr> <tr> <td>Vegetable</td><td>V DP</td><td>V I</td><td>V Th</td></tr> <tr> <td>Chicken</td><td>C DP</td><td>C I</td><td>C Th</td></tr> <tr> <td>Tuna</td><td>T DP</td><td>T I</td><td>T Th</td></tr> </tbody> </table>		Deep pan	Italian	Thin	Cheese	C DP	C I	C Th	Mushroom	M DP	M I	M Th	Vegetable	V DP	V I	V Th	Chicken	C DP	C I	C Th	Tuna	T DP	T I	T Th
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Multiplication

Year 5	- Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers - Recognise and use square numbers and cube numbers, and the notation for squared (²) and cubed (³) - Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers. - Multiply numbers mentally drawing upon known facts. - Multiply whole numbers and those involving decimals by 10, 100 and 1000 - Multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams.																																
Progression of skills	Key representations																																
Multiples and factors Encourage children to notice patterns and make links with known facts.	... is a multiple of ... because ... × ... = ...  <table border="1" data-bbox="725 984 1104 1096"><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr><tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr></table>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	... is a factor of ... because ... × ... = ...  1×8  2×4 1, 2, 4 and 8 are factors of 8	The common factors of ... and ... are ... Factors of 20 Factors of 12 
1	2	3	4	5	6	7	8	9	10																								
11	12	13	14	15	16	17	18	19	20																								
21	22	23	24	25	26	27	28	29	30																								
Square and cube numbers	... squared means ... × ...  1×1 $1^2 = 1$  2×2 $2^2 = 4$  3×3 $3^2 = 9$  4×4 $4^2 = 16$		... cubed means ... × ... × ...  $1 \times 1 \times 1$ $1^3 = 1$  $2 \times 2 \times 2$ $2^3 = 8$  $3 \times 3 \times 3$ $3^3 = 27$																														

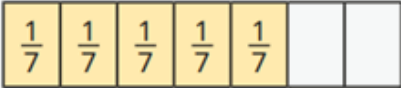
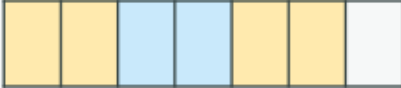
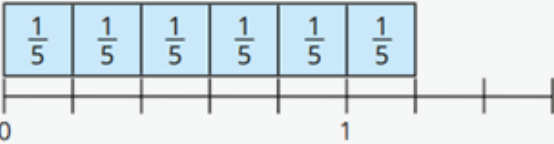
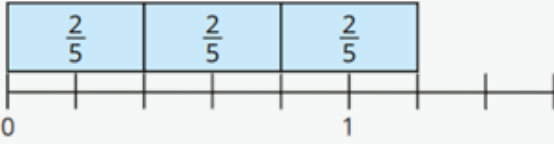
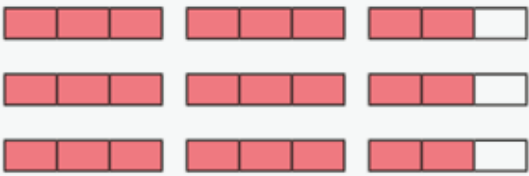
Multiplication

Progression of skills	Key representations																																																						
Multiply numbers up to 4 digits by a 1-digit number This builds on the short multiplication method introduced in Y4	To multiply a 4-digit number by ... , I multiply the ones by ... , the tens by ... , the hundreds by ... and the thousands by ... <table><tr><th>Th</th><th>H</th><th>T</th><th>O</th></tr><tr><td>1000</td><td>100</td><td>10 10 10</td><td>1 1</td></tr><tr><td>100</td><td>100</td><td>10 10 10</td><td>1 1</td></tr><tr><td>100</td><td>100</td><td>10 10</td><td>1 1</td></tr></table><table><tr><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td>1</td><td>1</td><td>5</td><td>2</td></tr><tr><td>x</td><td></td><td></td><td></td><td>3</td></tr><tr><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td></td></tr></table>		Th	H	T	O	1000	100	10 10 10	1 1	100	100	10 10 10	1 1	100	100	10 10	1 1							1	1	5	2	x				3																						
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x				3																																																			
Multiply numbers up to 4 digits by a 2-digit number Numbers are first partitioned using an area model then long multiplication is introduced for the first time.	I can partition ... into ... and ... <table><tr><td>x</td><td>40</td><td>4</td></tr><tr><td>30</td><td>1,200</td><td>120</td></tr><tr><td>2</td><td>80</td><td>8</td></tr></table> $32 \times 44 = 1,200 + 80 + 120 + 8$ $32 \times 44 = 1,408$	x	40	4	30	1,200	120	2	80	8	First, I multiply by the ... Then I multiply by the ... <table><tr><td>x</td><td>10</td><td>3</td></tr><tr><td>30</td><td>300</td><td>90</td></tr><tr><td>2</td><td>20</td><td>6</td></tr></table><table><tr><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>3</td><td>2</td><td></td></tr><tr><td>x</td><td></td><td>1</td><td>3</td><td></td></tr><tr><td></td><td></td><td>9</td><td>6</td><td></td></tr><tr><td></td><td>3</td><td>2</td><td>0</td><td></td></tr><tr><td></td><td>4</td><td>1</td><td>6</td><td></td></tr><tr><td></td><td></td><td></td><td></td><td></td></tr></table> (32 x 3) (32 x 10) 300 + 90 + 20 + 6 = 416	x	10	3	30	300	90	2	20	6								3	2		x		1	3				9	6			3	2	0			4	1	6						
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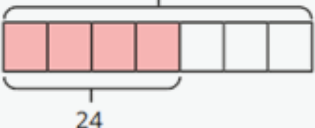
Multiplication

Progression of skills	Key representations																										
Multiply by 10, 100 and 1,000 Some children may over-generalise that multiplying by a power of 10 always results in adding zeros. This will cause issues later when multiplying decimals.	To multiply by 10/100/1,000, I move all the digits ... places to the left. ... is 10/100/1,000 times the size of ... <table><tr><th>M</th><th>HTh</th><th>TTh</th><th>Th</th><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td></td><td></td><td></td><td>●●</td><td>●●●</td><td>●●●</td></tr></table><table><tr><th>Th</th><th>H</th><th>T</th><th>O</th><th>Tth</th><th>Hth</th></tr><tr><td></td><td></td><td></td><td>●●</td><td>●●●</td><td>●●●</td></tr></table> $234 \times 10 = 2,340$ $234 \times 100 = 23,400$ $234 \times 1,000 = 234,000$ $2.34 \times 10 = 23.4$ $2.34 \times 100 = 234$ $2.34 \times 1,000 = 2,340$	M	HTh	TTh	Th	H	T	O					●●	●●●	●●●	Th	H	T	O	Tth	Hth				●●	●●●	●●●
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Mental strategies Children continue to use efficient mental strategies such as partitioning and knowledge of factor pairs and related facts to multiply.	The most efficient strategy to calculate ... $\times$... is ... To calculate ... $\times$ 12, I can do ... $\times$... $\times$... For example: 121×12 I could calculate 100×12 plus 20×12 plus 1×12 I could calculate 121×10 plus 121×2 I could calculate $121 \times 6 \times 2$ I could calculate $121 \times 4 \times 3$																										

Multiplication

Progression of skills	Key representations
Multiply fractions by a whole number Make links with repeated addition. E.g. $\frac{1}{5} \times 4 = \frac{1}{5} + \frac{1}{5} + \frac{1}{5} + \frac{1}{5}$	To multiply a fraction by an integer, I multiply the numerator by the integer and the denominator remains the same.  $\frac{1}{7} \times 5 = \frac{1}{7} + \frac{1}{7} + \frac{1}{7} + \frac{1}{7} + \frac{1}{7} = \frac{5}{7}$  $\frac{2}{7} \times 3 = \frac{2}{7} + \frac{2}{7} + \frac{2}{7} = \frac{6}{7}$  $\frac{1}{5} \times 6 = \frac{6}{5} = 1\frac{1}{5}$  $\frac{2}{5} \times 3 = \frac{6}{5} = 1\frac{1}{5}$
Multiply mixed numbers by a whole number	I can partition $\frac{\square}{\square}$ into $\frac{\square}{\square}$ and $\frac{\square}{\square}$  $2\frac{2}{3} \times 3$ $2 \times 3 = 6 \quad \frac{2}{3} \times 3 = \frac{6}{3} = 2$ $2\frac{2}{3} \times 3 = 6 + 2 = 8$

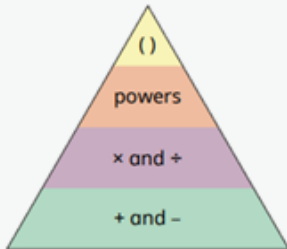
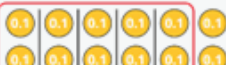
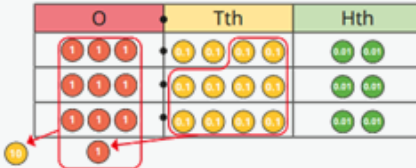
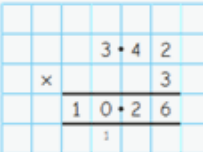
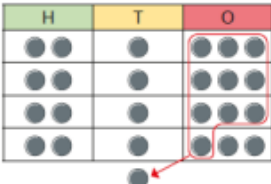
Multiplication

Progression of skills	Key representations	
Find the whole Children multiply to find the whole from a given part.	If $\frac{1}{\square}$ is ... , then the whole is ... $\times$... $\frac{1}{5}$ of ___ = 6  $5 \times 6 = 30$ $\frac{1}{5}$ of 30 = 6	If $\frac{\square}{\square}$ is ... , then $\frac{1}{\square}$ is ... and the whole is ... $\times$... $\frac{4}{7}$ of ___ = 24  $\frac{1}{7} = 24 \div 4 = 6$ $7 \times 6 = 42$ $\frac{4}{7}$ of 42 = 24

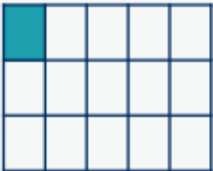
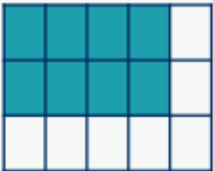
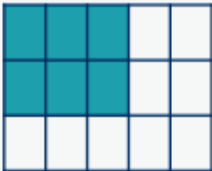
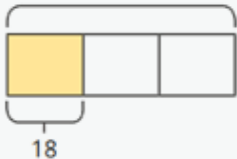
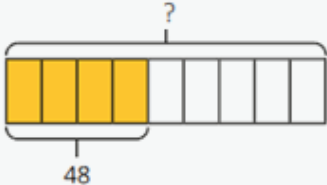
Multiplication

Year 6	- Identify common factors and common multiples. - Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication. - Multiply numbers by 10, 100 and 1,000 - Multiply one-digit numbers with up to two decimal places by whole numbers. - Use their knowledge of the order of operations to carry out calculations involving the 4 operations. - Multiply simple pairs of proper fractions, writing the answer in its simplest form. - Solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts. - Solve problems involving the calculation of percentages.																																																								
Progression of skills	Key representations																																																								
Multiply numbers up to 4 digits by a 2-digit number	To multiply by a 2-digit number, first multiply by the ones, then multiply by the tens and then find the total. <table><tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td>1</td><td>2</td><td>0</td><td>7</td><td></td></tr><tr><td></td><td>×</td><td></td><td></td><td></td><td>3</td><td>6</td><td></td></tr><tr><td>+</td><td></td><td>7</td><td>2</td><td>4</td><td>2</td><td></td><td>(1,207 × 6)</td></tr><tr><td></td><td>3</td><td>6</td><td>2</td><td>1</td><td>0</td><td></td><td>(1,207 × 30)</td></tr><tr><td></td><td>4</td><td>3</td><td>4</td><td>5</td><td>2</td><td></td><td></td></tr><tr><td></td><td>1</td><td></td><td></td><td></td><td></td><td></td><td></td></tr></table>												1	2	0	7			×				3	6		+		7	2	4	2		(1,207 × 6)		3	6	2	1	0		(1,207 × 30)		4	3	4	5	2				1						
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Multiply by 10, 100 and 1,000	To multiply by 10/100/1,000, I move all the digits ... places to the left. ... is 10/100/1,000 times the size of ... <table><tr><td>M</td><td>HTh</td><td>TTh</td><td>Th</td><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td><td></td><td>●●</td><td>●●</td><td>●●</td></tr></table> $234 \times 10 = 2,340$ $234 \times 100 = 23,400$ $234 \times 1,000 = 234,000$ <table><tr><td>Th</td><td>H</td><td>T</td><td>O</td><td>Tth</td><td>Hth</td><td>Thth</td></tr><tr><td></td><td></td><td></td><td></td><td>●●</td><td>●●</td><td>●●</td></tr></table> $0.234 \times 10 = 2.34$ $0.234 \times 100 = 23.4$ $0.234 \times 1,000 = 234$	M	HTh	TTh	Th	H	T	O					●●	●●	●●	Th	H	T	O	Tth	Hth	Thth					●●	●●	●●																												
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Multiplication

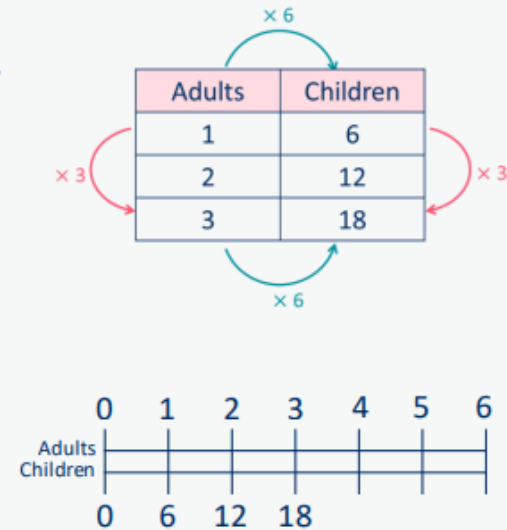
Progression of skills	Key representations	
Order of operations Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction.	... has greater priority than ..., so the first part of the calculation I need to do is ...   $(3 + 4) \times 2 = 14$  $3 + 4^2 = 19$  $3 + 4 \times 2 = 11$	
Multiply decimals by integers This is the first time children multiply decimals by numbers other than 10, 100 or 1,000. Encourage them to make links with known facts and whole number multiplication.	I know that ... $\times$... = ..., so I also know that ... $\times$... = ...  $6 \times 2 = 12$  $6 \times 0.2 = 1.2$	I need to exchange 10 ... for 1 ...    $213 \times 4 = 852$  $2.13 \times 4 = 8.52$

Multiplication

Progression of skills	Key representations	
Multiply fractions by fractions Encourage children to give answers in their simplest form.	When multiplying a pair of fractions, I need to multiply the numerator and multiply the denominator.  $\frac{1}{3} \times \frac{1}{5} = \frac{1}{15}$  $\frac{2}{3} \times \frac{4}{5} = \frac{8}{15}$  $\frac{2}{3} \times \frac{3}{5} = \frac{6}{15} = \frac{2}{5}$	
Find the whole Children multiply to find the whole from a given part.	If $\frac{1}{\square}$ is ... , then the whole is ... $\times$... $\frac{1}{3}$ of $\underline{\quad}$ = 18  $18 \times 3 = 54$ $\frac{1}{3}$ of 54 = 18	If $\frac{\square}{\square}$ is ... , then $\frac{1}{\square}$ is ... and the whole is ... $\times$... $\frac{4}{9}$ of $\underline{\quad}$ = 48  $\frac{1}{9} = 48 \div 4 = 12$ $9 \times 12 = 108$ $\frac{4}{9}$ of 108 = 48

Multiplication

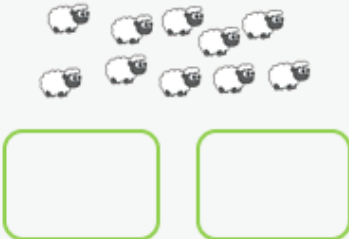
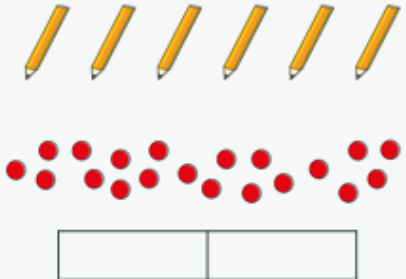
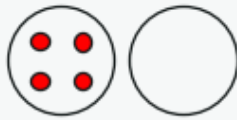
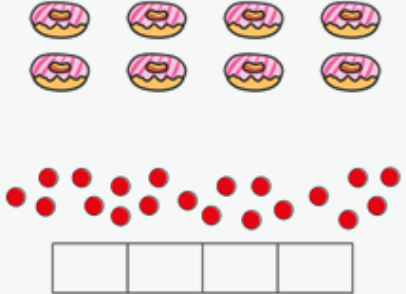
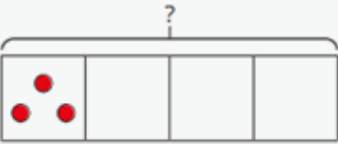
Progression of skills	Key representations																																	
Calculate percentages Children first learn how to find 1%, 10%, 20%, 25% and 50% before using multiples of these amounts to find any percentage.	There are ... lots of ... % in 100% To find ... %, I need to divide by ... <table border="1"><tr><td colspan="4">100%</td></tr><tr><td colspan="2">50%</td><td colspan="2">50%</td></tr><tr><td>25%</td><td>25%</td><td>25%</td><td>25%</td></tr></table> 50% of ... = ... ÷ 2 25% of ... = ... ÷ 4	100%				50%		50%		25%	25%	25%	25%	... % is made up of ... %, and ... % <table border="1"><tr><td colspan="10">100%</td></tr><tr><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td></tr></table> To find 30%, I can find 10% and then multiply it by 3 To find 23%, I can use 10% × 2 and 1% × 3 To find 99%, I can find 1%, then subtract from 100%	100%										10%	10%	10%	10%	10%	10%	10%	10%	10%	10%
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Calculations involving ratio Encourage children to see the multiplicative relationship between ratios. They will need to multiply or divide each value by the same number to keep the ratio equivalent. Double number lines and ratio tables help children to see both horizontal and vertical multiplicative relationships.	For every ... , there are ... For every 1 adult on a school trip, there are 6 children. adults <table border="1"><tr><td></td></tr></table> children <table border="1"><tr><td></td><td></td><td></td><td></td><td></td><td></td></tr></table>								<table border="1"><tr><td>Adults</td><td>Children</td></tr><tr><td>1</td><td>6</td></tr><tr><td>2</td><td>12</td></tr><tr><td>3</td><td>18</td></tr></table> × 3 × 6 × 6 × 3 0 1 2 3 4 5 6 Adults Children 0 6 12 18	Adults	Children	1	6	2	12	3	18																	
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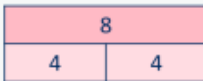
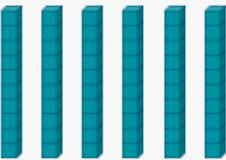
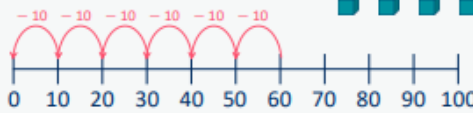
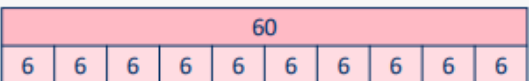
Division

Year 1	- Solve simple one-step problems involving division, using concrete objects, pictorial representations and arrays with the support of the teacher. - Recognise, find and name a half as one of two equal parts of a quantity. - Recognise, find and name a quarter as one of four equal parts of an object, shape or quantity.		
Progression of skills	Key representations		
Make equal groups - grouping Encourage children to physically move objects into equal groups. They can also circle equal groups when using pictures.	There are ... altogether. How many groups of ... can you make?  	Circle groups of 2 There are ... groups of 2 	Take ... cubes. Make equal groups.  There are ... groups of ...
Make equal groups – sharing Encourage children to check that the objects have been shared fairly and each group is the same.	... have been shared equally between... There are ... on/in each ...    		Take ... cubes. Share them between ...  12 shared between ... is ...

Division

Progression of skills	Key representations		
Find a half Start with practical opportunities to share a quantity into 2 groups. Progress to circling half of the objects in a picture and then to finding the whole from a given half.	To find half, I need to share into 2 equal groups.  There are ... in each group.	Half of ... is ...  There are ... in each group.	If ... is half, what is the whole?  4 is half of ...
Find a quarter Start with practical opportunities to share a quantity into 4 groups. Progress to using pictures or bar models to find a quarter and then to finding the whole from a given quarter.	To find a quarter, I need to share into 4 equal groups.  There are ... in each group.	A quarter of ... is ...  There are ... in each group.	If ... is one quarter, what is the whole?  3 is one quarter of ...

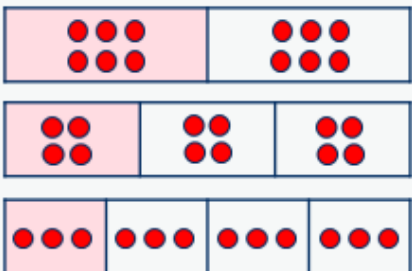
Division

Year 2	- Recall and use division facts for the 2, 5 and 10 multiplication tables. - Calculate mathematical statements for division within the multiplication tables and write them using the division ($\div$) and equals ($=$) signs. - Recognise, find, name and write fractions $\frac{1}{3}$, $\frac{1}{4}$, $\frac{2}{4}$ and $\frac{3}{4}$ of a quantity.	
Progression of skills	Key representations	
Divide by 2 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts and halving.	There are ... equal groups of 2 ... $\div 2 =$...  $4 \times 2 = 8$ $8 \div 2 = 4$  	... shared equally between 2 is ... Half of ... is $\div 2 =$...  $4 \times 2 = 8$ $8 \div 2 = 4$   
Divide by 10 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are ... equal groups of 10 ... $\div 10 =$... $6 \times 10 = 60$ $60 \div 10 = 6$  	... shared equally between 10 is $\div 10 =$... $6 \times 10 = 60$ $60 \div 10 = 6$  

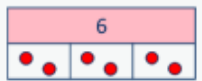
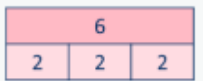
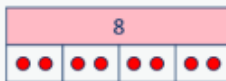
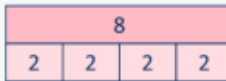
Division

Progression of skills	Key representations	
Divide by 5 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are ... equal groups of 5 ... $\div 5 = \dots$ $6 \times 5 = 30$ $30 \div 5 = 6$	... shared equally between 5 is $\div 5 = \dots$ $6 \times 5 = 30$ $30 \div 5 = 6$
Missing numbers Bar models are useful to show the link between multiplication and division.	... divided by 2/5/10 is equal to ... $\square \div 2 = 10$ $\square \div 5 = 10$ $\square \div 10 = 10$	

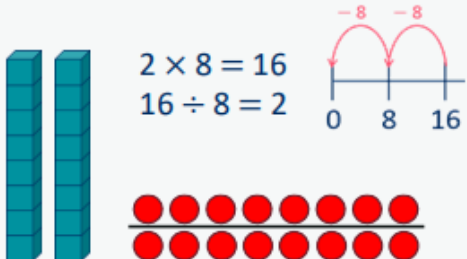
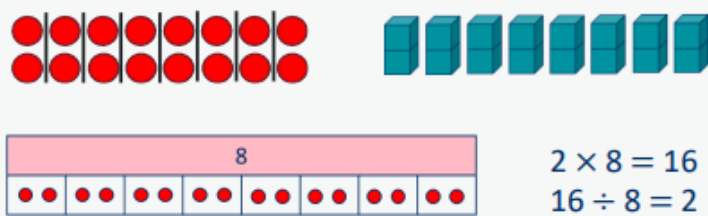
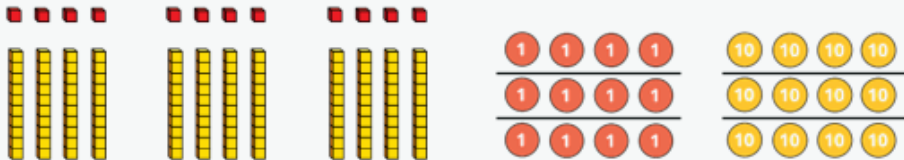
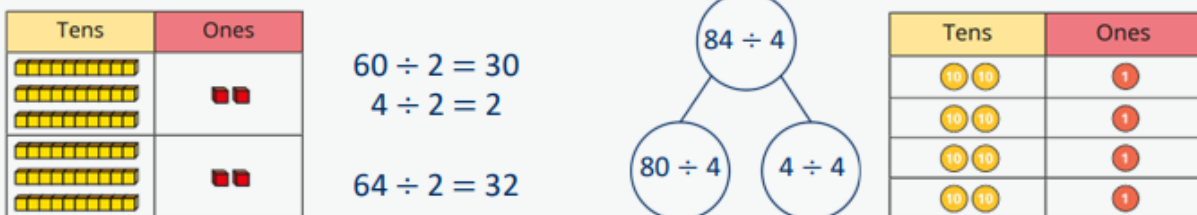
Division

Progression of skills	Key representations	
Unit fractions In Y2 the focus is on finding $\frac{1}{2}$, $\frac{1}{4}$ and $\frac{1}{3}$ Bar models are useful to show the link between division and finding a fraction.	The objects have been shared fairly into ... groups. $\frac{1}{\square}$ of ... is ... 	There are ... equal parts. There is ... part circled. $\frac{1}{\square}$ is circled. 
Non-unit fractions In Y2 the focus is on finding $\frac{2}{4}$ and $\frac{3}{4}$ Prompt children to notice that $\frac{2}{4}$ is equivalent to $\frac{1}{2}$	The objects have been shared fairly into ... groups. $\frac{\square}{\square}$ of ... is ... 	There are ... equal parts. There are ... parts circled. $\frac{\square}{\square}$ is circled. 

Division

Year 3	- Recall and use division facts for the 3, 4 and 8 multiplication tables. - Write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods. - Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators.	
Progression of skills	Key representations	
Divide by 3 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are ... groups of 3 in ... $\dots \div 3 =$  $2 \times 3 = 6$ $6 \div 3 = 2$  	... has been shared equally into 3 equal groups. $\dots \div 3 =$  $2 \times 3 = 6$ $6 \div 3 = 2$   
Divide by 4 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are ... groups of 4 in ... $\dots \div 4 =$  $2 \times 4 = 8$ $8 \div 4 = 2$  	... has been shared equally into 4 equal groups. $\dots \div 4 =$  $2 \times 4 = 8$ $8 \div 4 = 2$   

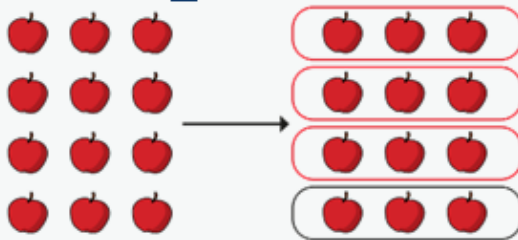
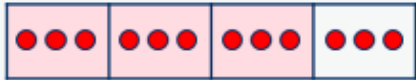
Division

Progression of skills	Key representations	
Divide by 8 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are ... groups of 8 in ... $\dots \div 8 =$  $2 \times 8 = 16$ $16 \div 8 = 2$	... has been shared equally into 8 equal groups. $\dots \div 8 =$  $2 \times 8 = 16$ $16 \div 8 = 2$
Related facts Link to known times-table facts.	... $\div$... is equal to ..., so ... tens $\div$... is equal to ... tens.  $12 \div 3 = 4$ $120 \div 3 = 40$	
Divide a 2-digit number by a 1-digit number - no exchange Partition into tens and ones to divide and then recombine.	... tens divided by ... is equal to ... tens. ... ones divided by ... is equal to ... ones.  $60 \div 2 = 30$ $4 \div 2 = 2$ $64 \div 2 = 32$ $84 \div 4$ $80 \div 4$ $4 \div 4$ $80 \div 4 = 20$ $4 \div 4 = 1$ $84 \div 4 = 21$	

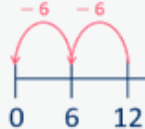
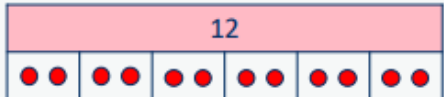
Division

Progression of skills	Key representations																																					
Divide a 2-digit number by a 1-digit number - with remainders Encourage children to partition numbers flexibly to help them to divide more efficiently.	... tens divided by ... is equal to ... tens. ... ones divided by ... is equal to ... ones. <table><thead><tr><th>Tens</th><th>Ones</th></tr></thead><tbody><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></tbody></table> 96 ÷ 4 80 ÷ 4 16 ÷ 4 80 ÷ 4 = 20 16 ÷ 4 = 4 96 ÷ 4 = 24	Tens	Ones											There are ... groups of ... There are ... remaining. 31 ÷ 4 = 7 r3 94 ÷ 4 = 23 r2 <table><thead><tr><th>Tens</th><th>Ones</th></tr></thead><tbody><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></tbody></table><table><thead><tr><th>Tens</th><th>Ones</th></tr></thead><tbody><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></tbody></table>	Tens	Ones											Tens	Ones										
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Unit fractions of a set of objects Bar models are useful to show the link between division and fractions, for example, dividing by 3 and finding a third.	The whole is divided into ... equal parts. Each part is $\frac{1}{\square}$ of the whole. $\frac{1}{4}$ of 12 apples is 3 apples.	One ... of ... is ... $\frac{1}{4}$ of 12 is 3 $\frac{1}{3}$ of 36 is 12																																				

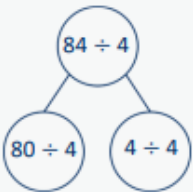
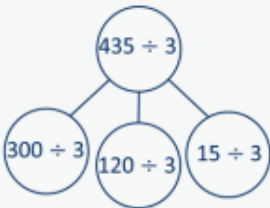
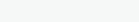
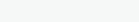
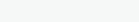
Division

Progression of skills	Key representations	
Non-unit fractions of a set of objects Bar models are a useful representation and show the links with division and multiplication.	The whole is divided into ... equal parts. Each part is $\frac{1}{\square}$ of the whole.  $\frac{3}{4}$ of 12 apples is 9 apples.	$\frac{1}{\square}$ of ... is ..., so $\frac{\square}{\square}$ of ... is ... $\frac{3}{4}$ of 12 is 9  $\frac{2}{3}$ of 36 is 24 

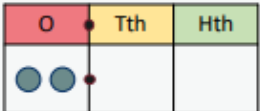
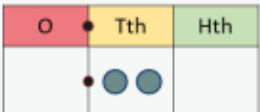
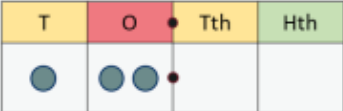
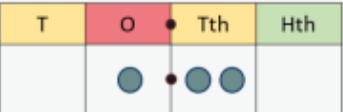
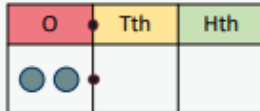
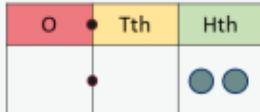
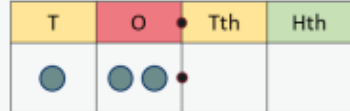
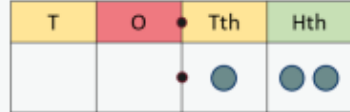
Division

Year 4	- Recall division facts for multiplication tables up to 12×12 - Use place value, known and derived facts to divide mentally, including: dividing by 1 - Find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths.	
Progression of skills	Key representations	
Division facts to 12×12 Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are ... groups of ... in ... $\dots \div \dots =$   $2 \times 6 = 12$ $12 \div 6 = 2$ 	... has been shared equally into ... equal groups. $\dots \div \dots =$    $2 \times 6 = 12$ $12 \div 6 = 2$
Divide a number by 1 and itself Children may try to divide a number by zero and it should be highlighted that this is not possible.	When I divide a number by 1, the number remains the same. 5 shared between 1 is 5  There are 5 groups of 1 in 5 	When I divide a number by itself, the answer is 1 5 shared between 5 is 1  There is 1 group of 5 in 5 

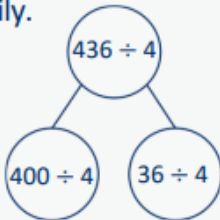
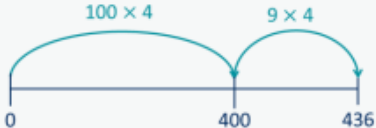
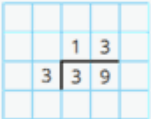
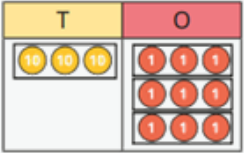
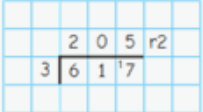
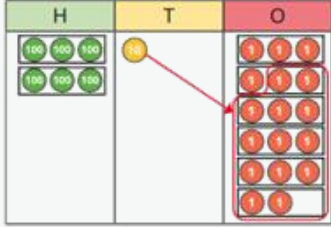
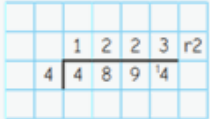
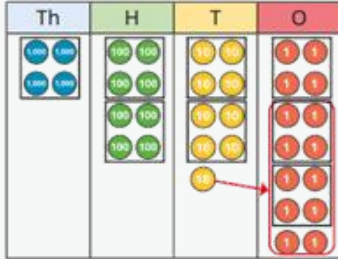
Division

Progression of skills	Key representations																										
Related facts Link to known times-table facts.	... ÷ ... is equal to ... so ... tens ÷ ... is equal to ... tens and ... hundreds ÷ ... is equal to ... hundreds.    $21 \div 7 = 3$ $210 \div 7 = 30$ $2,100 \div 7 = 300$ $21 \div 3 = 7$ $210 \div 3 = 70$ $2,100 \div 3 = 700$																										
Divide a 2 or 3-digit number by a 1-digit number Progress from divisions with no exchange, to divisions with exchange and then divisions with remainders.	I can partition ... into ... tens and ... ones.  $80 \div 4 = 20$ $4 \div 4 = 1$ $84 \div 4 = 21$ <table><thead><tr><th>Tens</th><th>Ones</th></tr></thead><tbody><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></tbody></table>	Tens	Ones									I cannot share the hundreds/tens equally, so I need to exchange 1 ... for 10 ...  $300 \div 3 = 100$ $120 \div 3 = 40$ $15 \div 3 = 5$ $435 \div 3 = 145$ <table><thead><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr></thead><tbody><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr></tbody></table>	Hundreds	Tens	Ones												
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Hundreds	Tens	Ones																									
																											
																											
																											
																											

Division

Progression of skills	Key representations			
Divide by 10 and 100 Encourage children to notice that dividing by 100 is the same as dividing by 10 twice.	When I divide by 10, the digits move 1 place value column to the right. ... is one-tenth the size of ...		When I divide by 100, the digits move 2 place value columns to the right. ... is one-hundredth the size of ...	
	  $2 \div 10 = 0.2$	  $12 \div 10 = 1.2$	  $2 \div 100 = 0.02$	  $12 \div 100 = 0.12$

Division

Year 5	- Divide numbers mentally drawing upon known facts. - Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context. - Divide whole numbers and those involving decimals by 10, 100 and 1,000		
Progression of skills	Key representations		
Mental strategies	I can partition ... into ... and ... to help me to divide more easily. 	I can show groups of ... on a number line. 	To divide by ..., I can divide by ... and then divide the result by ... $436 \div 4 = 436 \div 2 \div 2$ $436 \div 2 = 218$ $218 \div 2 = 109$
Divide numbers up to 4 digits by a 1-digit number The short division method is introduced for the first time.	There are ... groups of ... hundreds/tens/ones/ in ... I can exchange 1 ... for 10 ...      		

Division

Progression of skills	Key representations																																																	
Divide by 10, 100 and 1,000 Encourage children to notice that dividing by 100 is the same as dividing by 10 twice, and that dividing by 1,000 is the same as dividing by 10 three times.	To divide by 10/100/1,000, I move all the digits ... places to the right. ... is one-tenth/one-hundredth/one-thousandth the size of ... <table><tr><th>Th</th><th>H</th><th>T</th><th>O</th><th>Tth</th><th>Hth</th></tr><tr><td></td><td>●</td><td>●●</td><td></td><td>●</td><td></td></tr></table> <table><tr><th>Th</th><th>H</th><th>T</th><th>O</th><th>Tth</th><th>Hth</th></tr><tr><td></td><td></td><td>●</td><td>●●</td><td>●</td><td></td></tr></table> $120 \div 10 = 12$ <table><tr><th>Th</th><th>H</th><th>T</th><th>O</th><th>Tth</th><th>Hth</th></tr><tr><td></td><td></td><td></td><td>●</td><td>●●</td><td></td></tr></table> $120 \div 100 = 1.2$ <table><tr><th>Th</th><th>H</th><th>T</th><th>O</th><th>Tth</th><th>Hth</th></tr><tr><td></td><td></td><td></td><td></td><td>●</td><td>●●</td></tr></table> $120 \div 1,000 = 0.12$		Th	H	T	O	Tth	Hth		●	●●		●		Th	H	T	O	Tth	Hth			●	●●	●		Th	H	T	O	Tth	Hth				●	●●		Th	H	T	O	Tth	Hth					●	●●
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Fraction of an amount Bar models support children to understand that to find a fraction of an amount, we divide by the denominator and multiply by the numerator.	To find $\frac{\square}{\square}$ of ... , I need to divide by ... and multiply by ... <table><tr><td>●●</td><td>●●</td><td>●●</td><td>●●</td><td>●●</td></tr></table> <table><tr><td>10</td><td>10</td><td>10</td><td>10</td><td>10</td></tr><tr><td>1</td><td>1</td><td>1</td><td>1</td><td>1</td></tr></table> $\frac{1}{5}$ of 20 = $\frac{3}{5}$ of 20 = $\frac{1}{4}$ of 84 = $\frac{3}{4}$ of 84 =	●●	●●	●●	●●	●●	10	10	10	10	10	1	1	1	1	1	If $\frac{1}{\square}$ is ... , then the whole is ... $\times$... <table><tr><td colspan="5">?</td></tr><tr><td>6</td><td>6</td><td>6</td><td>6</td><td>6</td></tr></table> $\frac{1}{5}$ of ___ = 6 <table><tr><td colspan="5">?</td></tr><tr><td>■</td><td>■</td><td>■</td><td>■</td><td>■</td></tr></table> $\frac{4}{7}$ of ___ = 24	?					6	6	6	6	6	?					■	■	■	■	■													
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Division

Year 6	- Perform mental calculations, including with mixed operations and large numbers. - Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context. - Divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context. - Divide numbers by 10, 100 and 1,000 giving answers up to three decimal places. - Use written division methods in cases where the answer has up to two decimal places. - Associate a fraction with division and calculate decimal fraction equivalents. - Divide proper fractions by whole numbers [for example, $\frac{1}{3} \div 2 = \frac{1}{6}$] - Solve problems involving the calculation of percentages.
Progression of skills	Key representations
Short division Encourage children to interpret remainders in context, for example knowing that “4 remainder 1” could mean 4 complete boxes with 1 left over so 5 boxes will be needed.	There are ... groups of ... hundreds/tens/ones/ in ... I can exchange 1 ... for 10 ... The diagram shows four columns of base ten blocks labeled Th (Thousands), H (Hundreds), T (Tens), and O (Ones). The Th column has four blue blocks labeled 1,000. The H column has two green blocks labeled 100. The T column has one yellow block labeled 10 and three yellow blocks labeled 10. The O column has three red blocks labeled 1. A red box highlights one of the 1,000 blocks in the Th column, and a red arrow points from it to the T column, indicating an exchange of 1,000 for ten 100 blocks. The diagram shows a 2x5 grid of numbers. The top row contains the numbers 2, 1, 3, 1. The bottom row contains the numbers 4, 8, 5, 2, 4.

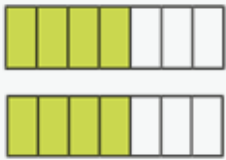
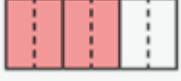
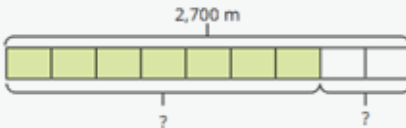
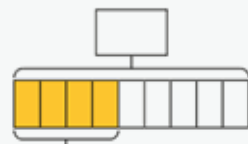
Division

Progression of skills	Key representations	
Mental strategies Include partitioning and number line strategies outlined in Y5 as well as division using factors.	To divide by ... , I can first divide by ... and then divide the answer by ... $240 \div 60 = 240 \div 10 \div 6$ $240 \rightarrow \boxed{\div 10} \rightarrow \boxed{} \rightarrow \boxed{\div 6} \rightarrow \boxed{}$ $480 \div 24 = 480 \div 4 \div 6$ $480 \rightarrow \boxed{\div 4} \rightarrow \boxed{} \rightarrow \boxed{\div 6} \rightarrow \boxed{}$ $9,120 \div 15 = 9,120 \div 5 \div 3$ 	
Long division The long division method is introduced for the first time. Two alternative methods are shown.	Method 1 	Method 2
Order of operations Calculations in brackets should be done first, then powers. Multiplication and division should be performed before addition and subtraction.	... has greater priority than ..., so the first part of the calculation I need to do is ...	

Division

Progression of skills	Key representations																																																																																																					
Divide by 10, 100 and 1,000 Encourage children to notice that dividing by 100 is the same as dividing by 10 twice, and that dividing by 1,000 is the same as dividing by 10 three times.	To divide by ... , I move the digits ... places to the right. <table><tr><th>H</th><th>T</th><th>O</th><th>Tth</th><th>Hth</th><th>Thth</th></tr><tr><td>●</td><td>●</td><td>●</td><td>●</td><td></td><td></td></tr></table> ÷ 1,000 <table><tr><th>H</th><th>T</th><th>O</th><th>Tth</th><th>Hth</th><th>Thth</th></tr><tr><td></td><td></td><td></td><td>●</td><td>●</td><td>●</td></tr></table> $312 \div 10 = 31.2$ $312 \div 100 = 3.12$ $312 \div 1,000 = 0.312$ $906 \div 10 = 90.6$ $906 \div 100 = 9.06$ $906 \div 1,000 = 0.906$		H	T	O	Tth	Hth	Thth	●	●	●	●			H	T	O	Tth	Hth	Thth				●	●	●																																																																												
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Divide decimals by integers This is the first time children divide decimals by numbers other than 10, 100 or 1,000	I know that ... ÷ ... = ..., so I also know that ... ÷ ... = ... <table><tr><td>10</td><td>1</td><td>1</td><td>1</td></tr><tr><td>10</td><td>1</td><td>1</td><td>1</td></tr><tr><td>10</td><td>1</td><td>1</td><td>1</td></tr></table>$39 \div 3 = 13$ <table><tr><td>1</td><td>0.1</td><td>0.1</td><td>0.1</td></tr><tr><td>1</td><td>0.1</td><td>0.1</td><td>0.1</td></tr><tr><td>1</td><td>0.1</td><td>0.1</td><td>0.1</td></tr></table>$3.9 \div 3 = 1.3$ <table><tr><td>0.1</td><td>0.01</td><td>0.01</td><td>0.01</td></tr><tr><td>0.1</td><td>0.01</td><td>0.01</td><td>0.01</td></tr><tr><td>0.1</td><td>0.01</td><td>0.01</td><td>0.01</td></tr></table>$0.39 \div 3 = 0.13$ I need to exchange 1 ... for 10 ... <table><tr><th>O</th><th>Tth</th><th>Hth</th></tr><tr><td>1</td><td>0.1</td><td>0.01</td></tr><tr><td>1</td><td>0.1</td><td>0.01</td></tr><tr><td>1</td><td>0.1</td><td>0.01</td></tr><tr><td>1</td><td>0.1</td><td>0.01</td></tr><tr><td>1</td><td>0.1</td><td>0.01</td></tr><tr><td>1</td><td>0.1</td><td>0.01</td></tr><tr><td>1</td><td>0.1</td><td>0.01</td></tr><tr><td>1</td><td>0.1</td><td>0.01</td></tr><tr><td>1</td><td>0.1</td><td>0.01</td></tr><tr><td>1</td><td>0.1</td><td>0.01</td></tr></table><table><tr><td>1</td><td>3</td><td>3</td></tr><tr><td>4</td><td>5</td><td>12</td></tr></table>		10	1	1	1	10	1	1	1	10	1	1	1	1	0.1	0.1	0.1	1	0.1	0.1	0.1	1	0.1	0.1	0.1	0.1	0.01	0.01	0.01	0.1	0.01	0.01	0.01	0.1	0.01	0.01	0.01	O	Tth	Hth	1	0.1	0.01	1	0.1	0.01	1	0.1	0.01	1	0.1	0.01	1	0.1	0.01	1	0.1	0.01	1	0.1	0.01	1	0.1	0.01	1	0.1	0.01	1	0.1	0.01	1	3	3	4	5	12																									
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Decimal and fraction equivalents	The fraction ... is equivalent to the decimal ... <table><tr><th colspan="10">1</th></tr><tr><td colspan="5">$\frac{1}{2}$</td><td colspan="5">$\frac{1}{2}$</td></tr><tr><td colspan="2">$\frac{1}{4}$</td><td colspan="2">$\frac{1}{4}$</td><td colspan="2">$\frac{1}{4}$</td><td colspan="2">$\frac{1}{4}$</td><td colspan="2">$\frac{1}{4}$</td></tr><tr><td colspan="2">$\frac{1}{5}$</td><td colspan="2">$\frac{1}{5}$</td><td colspan="2">$\frac{1}{5}$</td><td colspan="2">$\frac{1}{5}$</td><td colspan="2">$\frac{1}{5}$</td></tr><tr><td colspan="2">$\frac{1}{10}$</td><td colspan="2">$\frac{1}{10}$</td><td colspan="2">$\frac{1}{10}$</td><td colspan="2">$\frac{1}{10}$</td><td colspan="2">$\frac{1}{10}$</td></tr></table>$\frac{1}{5} = 0.2$$\frac{2}{5} = 0.4$$\frac{3}{5} = 0.6$ <table><tr><th colspan="10">1</th></tr><tr><td colspan="5">0.5</td><td colspan="5">0.5</td></tr><tr><td colspan="2">0.25</td><td colspan="2">0.25</td><td colspan="2">0.25</td><td colspan="2">0.25</td><td colspan="2">0.25</td></tr><tr><td colspan="2">0.2</td><td colspan="2">0.2</td><td colspan="2">0.2</td><td colspan="2">0.2</td><td colspan="2">0.2</td></tr><tr><td colspan="2">0.1</td><td colspan="2">0.1</td><td colspan="2">0.1</td><td colspan="2">0.1</td><td colspan="2">0.1</td></tr></table> × 25 $\frac{3}{4}$ $= \frac{75}{100} = 0.75$ × 25		1										$\frac{1}{2}$					$\frac{1}{2}$					$\frac{1}{4}$		$\frac{1}{4}$		$\frac{1}{4}$		$\frac{1}{4}$		$\frac{1}{4}$		$\frac{1}{5}$		$\frac{1}{5}$		$\frac{1}{5}$		$\frac{1}{5}$		$\frac{1}{5}$		$\frac{1}{10}$		$\frac{1}{10}$		$\frac{1}{10}$		$\frac{1}{10}$		$\frac{1}{10}$		1										0.5					0.5					0.25		0.25		0.25		0.25		0.25		0.2		0.2		0.2		0.2		0.2		0.1		0.1		0.1		0.1		0.1	
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Division

Progression of skills	Key representations		
Divide a fraction by an integer This is the first time children divide fractions by an integer.	... ones divided by 2 is ... ones so ... sevenths divided by 2 is ... sevenths.  $\frac{4}{7} \div 4 = \frac{1}{7}$ $\frac{4}{7} \div 2 = \frac{2}{7}$	I am dividing by ... , so I can split each part into ... equal parts.  $\frac{1}{3} \div 2 = \frac{1}{6}$	... is equivalent to ... so ... $\div$... = ... $\div$...  $\frac{2}{3} = \frac{4}{6}$ so $\frac{2}{3} \div 4 = \frac{4}{6} \div 4 = \frac{1}{6}$
Fraction of an amount Children divide and multiply to find fractions of an amount. Bar models can still be used to support understanding where needed.	To find $\frac{1}{\square}$ I divide by ... $\frac{1}{2} \text{ of } 36 = 36 \div 2$ $\frac{1}{12} \text{ of } 36 = 36 \div 12$	If $\frac{1}{\square}$ is equal to ..., then $\frac{\square}{\square}$ are equal to ...  $\frac{7}{9} \text{ of } 2,700 = \frac{1}{9} \text{ of } 2,700 \times 7$	If $\frac{\square}{\square}$ is equal to ..., then the whole is equal to ...  $\frac{4}{9} \text{ of } \underline{\quad} = 48$

Division

Progression of skills	Key representations																																	
Calculate percentages Children first learn how to find 1%, 10%, 20%, 25% and 50% before using multiples of these amounts to find any percentage.	There are ... lots of ... % in 100% To find ... %, I need to divide by ... <table border="1"><tr><td colspan="4">100%</td></tr><tr><td colspan="2">50%</td><td colspan="2">50%</td></tr><tr><td>25%</td><td>25%</td><td>25%</td><td>25%</td></tr></table> 50% of ... = ... ÷ 2 25% of ... = ... ÷ 4	100%				50%		50%		25%	25%	25%	25%	... % is made up of ... %, and ... % <table border="1"><tr><td colspan="10">100%</td></tr><tr><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td></tr></table> To find 30%, I can find 10% and then multiply it by 3 To find 23%, I can use 10% × 2 and 1% × 3 To find 99%, I can find 1%, then subtract from 100%	100%										10%	10%	10%	10%	10%	10%	10%	10%	10%	10%
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Calculations involving ratio Encourage children to see the multiplicative relationship between ratios. They will need to multiply or divide each value by the same number to keep the ratio equivalent. Double number lines and ratio tables help children to see both horizontal and vertical multiplicative relationships.	For every ... , there are ... For every 6 children on a school trip, there is 1 adult. adults  children 	<table border="1"><tr><th>Adults</th><th>Children</th></tr><tr><td>1</td><td>6</td></tr><tr><td>2</td><td>12</td></tr><tr><td>3</td><td>18</td></tr></table> ÷ 6 ÷ 3 ÷ 6 ÷ 3 Adults Children 0123456 061218	Adults	Children	1	6	2	12	3	18																								
Adults	Children																																	
1	6																																	
2	12																																	
3	18																																	
	The ratio of children to adults is 6 : 1																																	

The St Marys Church of England Primary School Values linked to Maths

Peace	Friendship	Respect	Trust	Perseverance
				
Using my mathematical knowledge to develop my responsibility to look after the world.	Sharing manipulatives responsibly and fairly during the maths lesson.	Respect the ideas of others and communicate my thoughts and ideas confidently and respectfully.	Trust in myself that I can achieve and make a difference.	Keep trying when skills are challenging.
Become responsible citizens through learning about how maths occurs in our environment.	Working together and collaborating to develop knowledge and understanding.	Understand the importance of our own responsibility within the world.	Trust that my knowledge will give me confidence to inspire others.	Develop my reasoning and problem-solving skills when learning mathematical concepts.
Ask thoughtful questions to develop my understanding of key mathematical concepts.	Understand how maths can be used to benefit the world and its people.	Be respectful and responsible when using mathematical equipment.	Trust that I can work effectively with others to strengthen my own understanding and develop others around me.	Aspire to be a fantastic mathematician.